

CLEO 2013 CF2I.7 @ Room C3 & C4 (San Jose Convention Center)



# High-Q sapphire WGM cavities fabricated by crystal growth

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# Outline



- ✓ Introduction
- ✓ Fabrication & optical measurement of crystalline WGM cavities
- ✓ Numerical analysis
- ✓ Summary

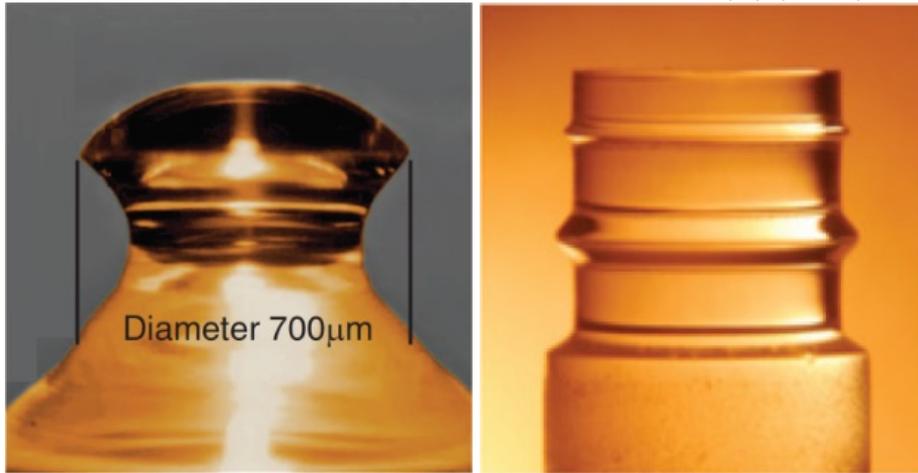
# High Q/V crystalline WGM cavity fabrication



## Crystalline cavities fabricated w/ precise machining

C. Y. Wang *et al.*, Nature Commun. **4**, 1345 (2013).

J. Hofer *et al.*, Phys. Rev. A **82**, 031804(R) (2010).

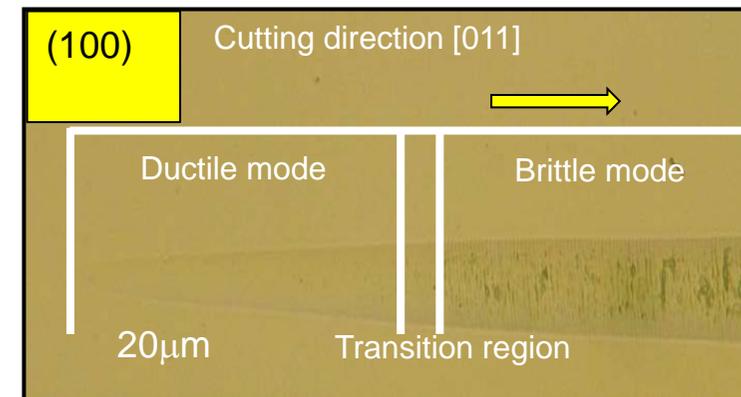
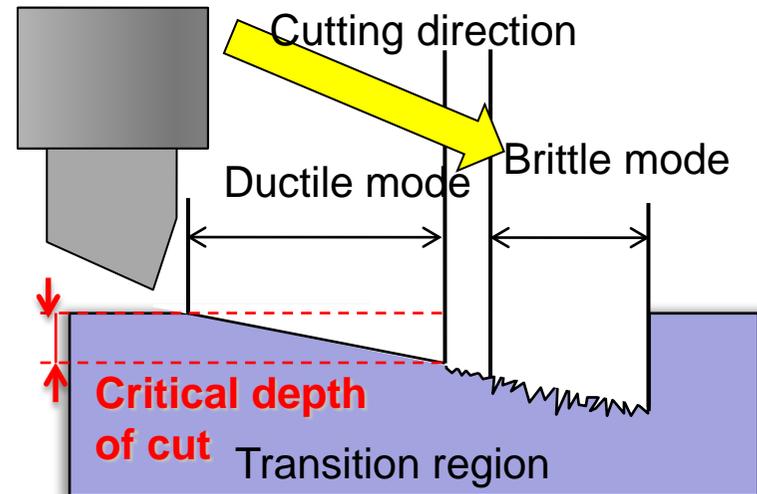


Q factor:  $10^9 \sim 10^{10}$   
Size: mm order

- ✓ Expensive machining needed
- ✓ Difficult to make small cavity

## Precise machining processing

Y. Mizumoto, *et al.*, Procedia Eng. **19**, 264 (2011).

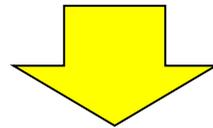


➤ brittle, fragile and inflexible



## Motivation

- ✓ Easy & inexpensive fabrication
- ✓ Fabrication of small cavity



**Laser-heated pedestal growth (LHPG)**

- ① Fabricate crystalline WGM cavity
- ② Achieve cross-sectional shape control
- ③ Understand effect of different cross-sections  
(circular → hexagonal)

# Laser-heated pedestal growth (LHPG)



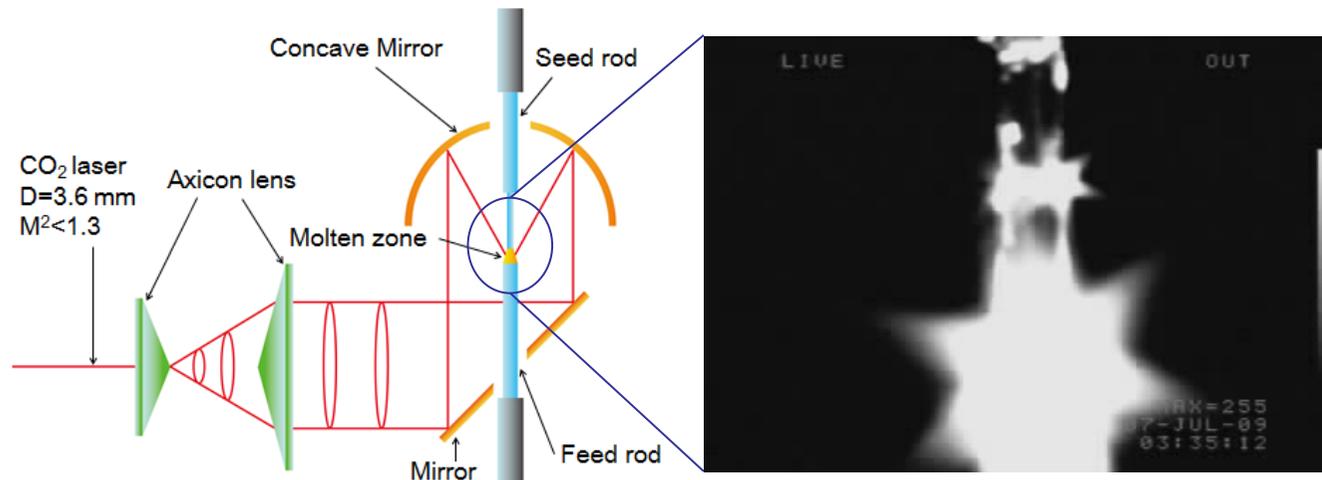
## Original LHPG:

- ✓ Fabrication of uniform crystal rods possible
- ✓ Fabrication of rods w/ diameter  $< 100 \mu\text{m}$  possible
- ✓ Fabrication of rods w/ smooth surface possible

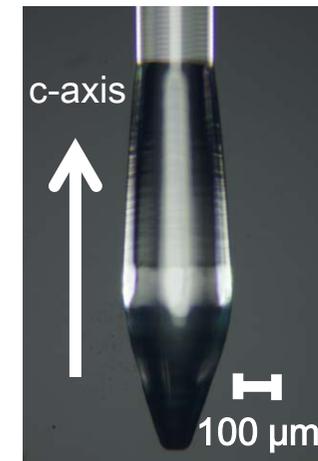
## Modified LHPG:

- ✓ Form bulge by **changing growth rate** (it allows WGM excitation)

### Experimental setup



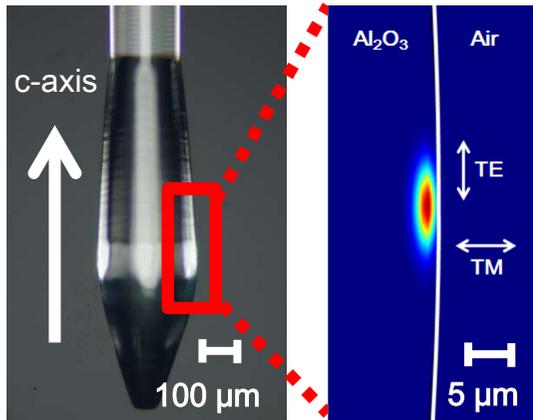
### Fabricated cavity



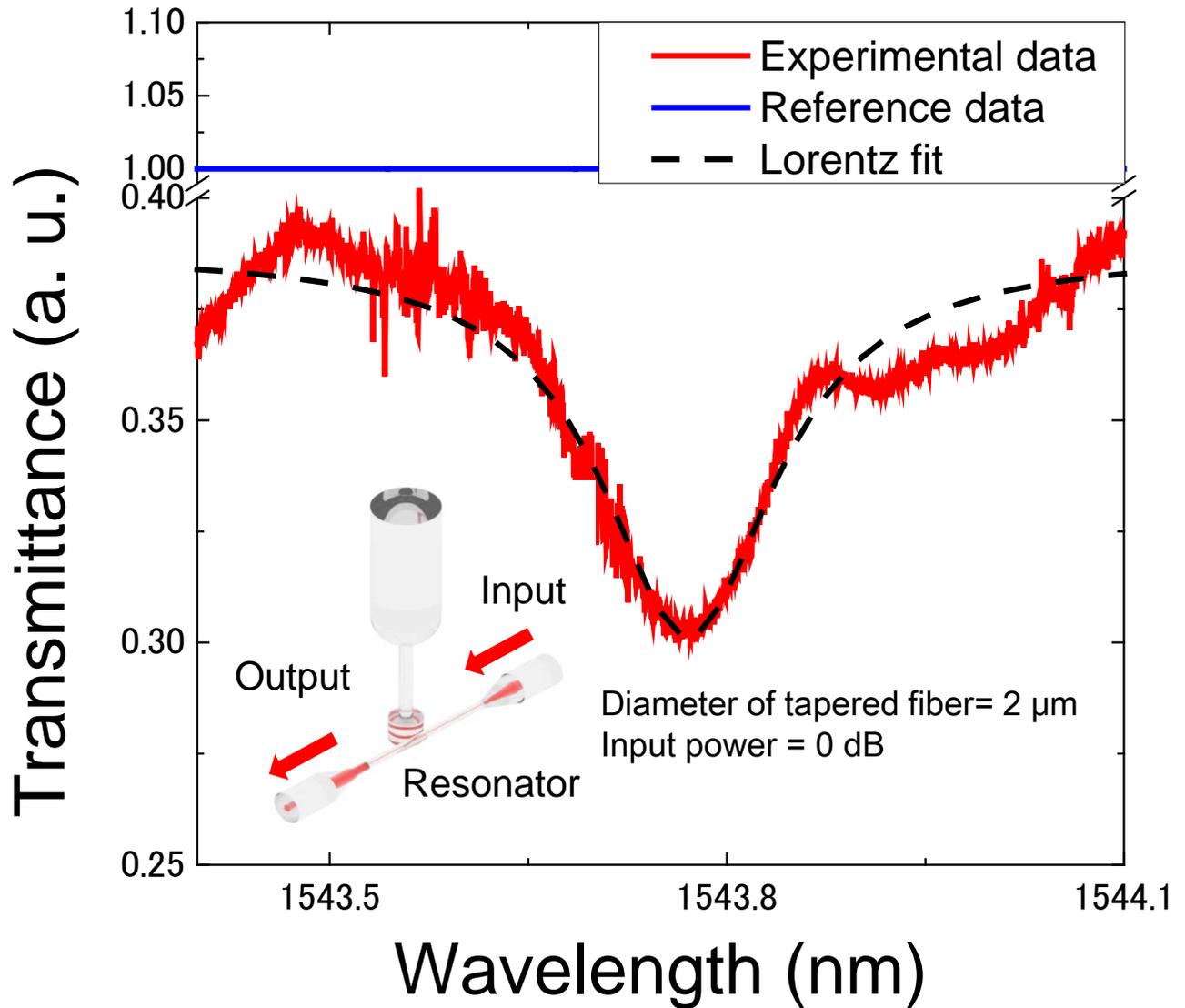
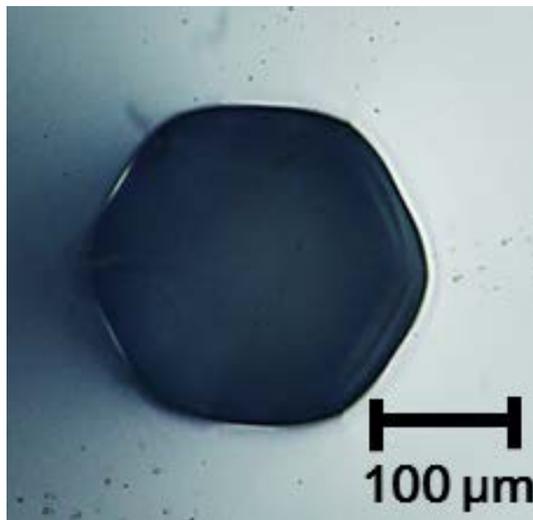
$$D_{grown} = D_{feed} \times \sqrt{v_{feed}/v_{seed}}$$

✓ **WGM cavity fabricated**

# Optical characteristics

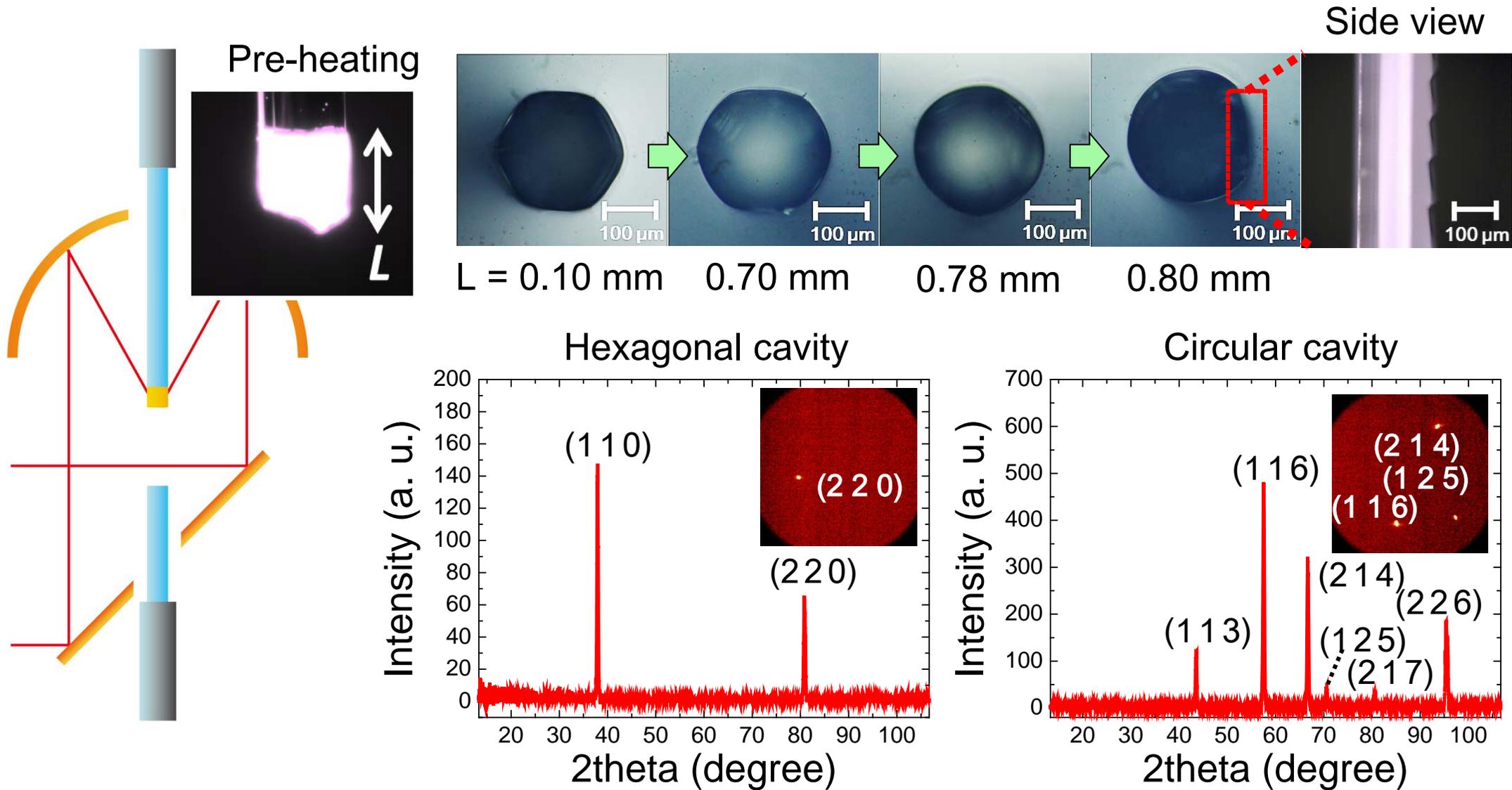


$$V_{\text{eff}} = 1.28 \times 10^{-2} \text{ mm}^3$$



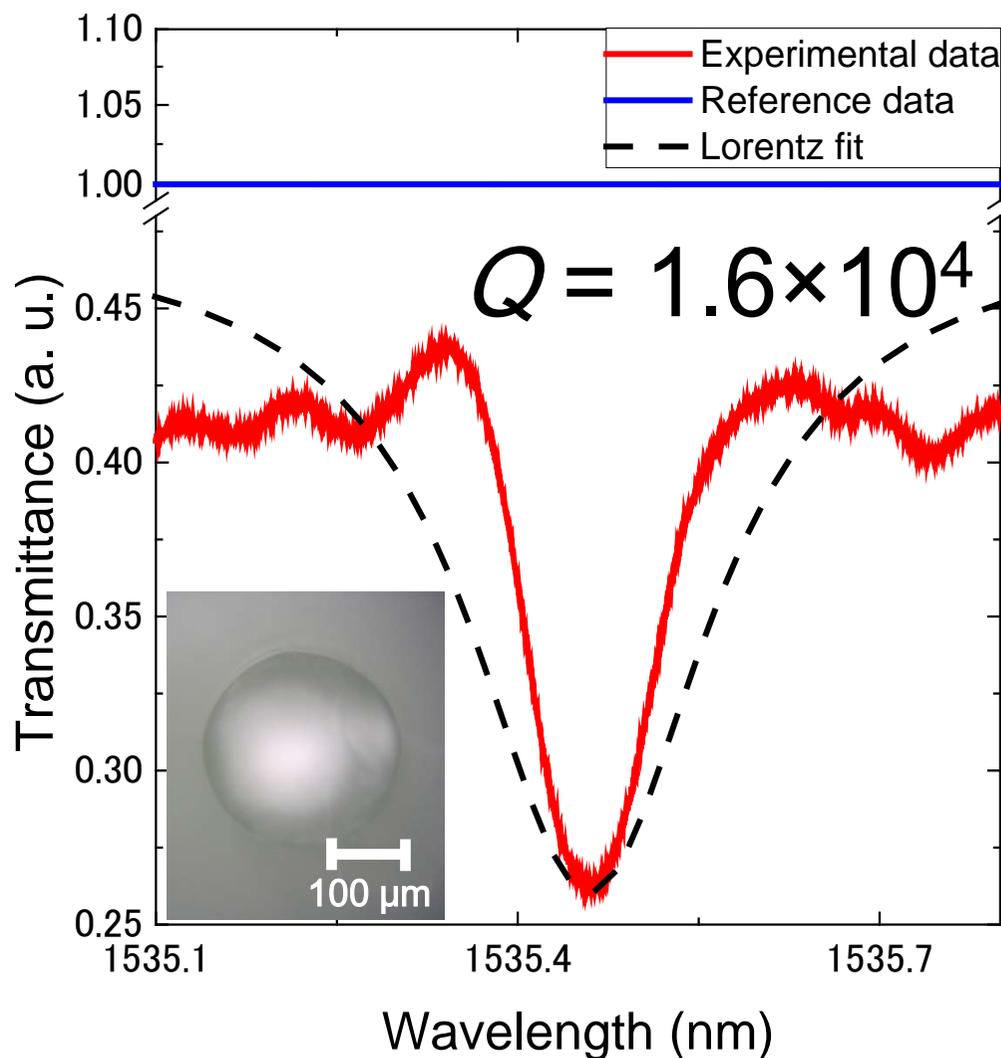
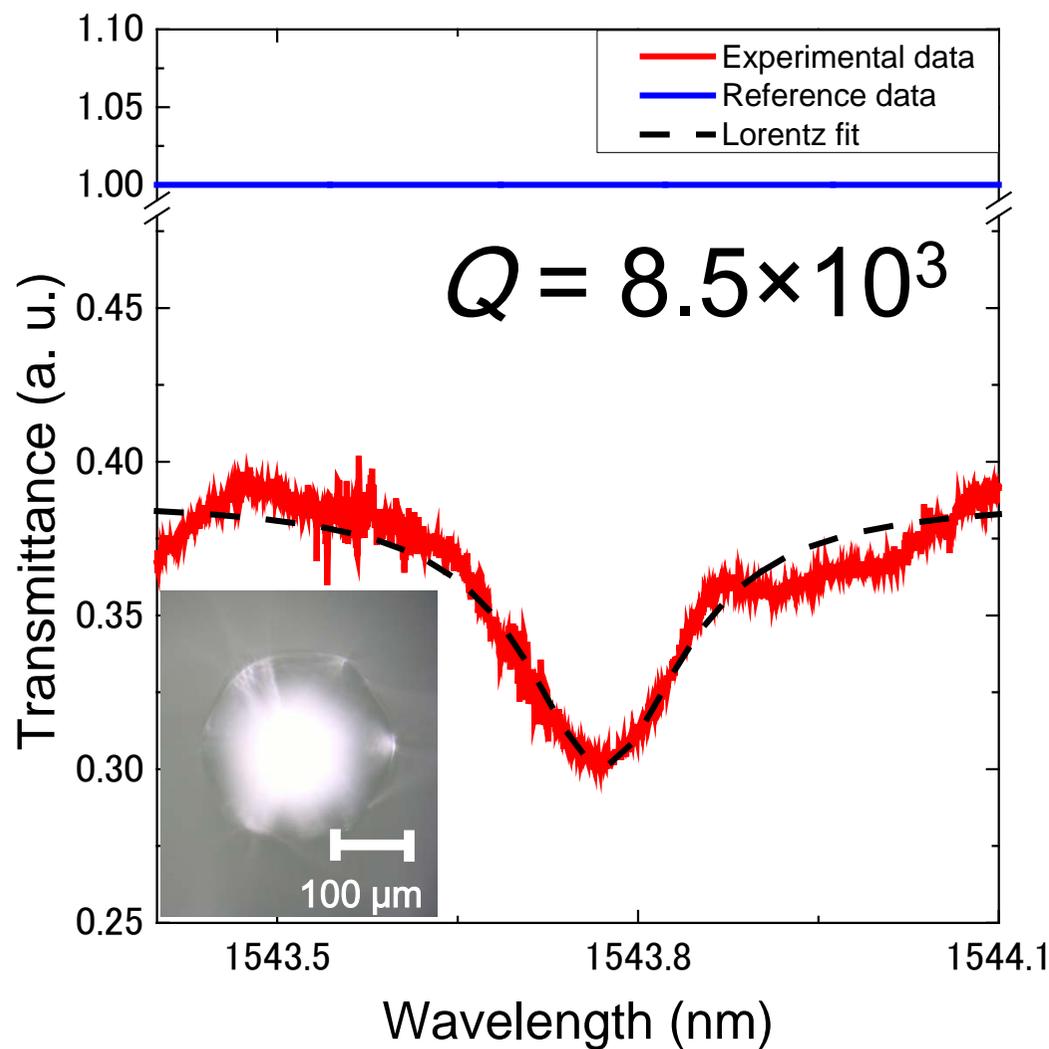
- ✓  $Q = 8.5 \times 10^3$  achieved
- ✓ Is cross-sectional shape critical to achieve high  $Q$ ?

# Pre-heating method: cross-sectional shape control



✓ Cross-sectional shape control demonstrated

# Optical measurement

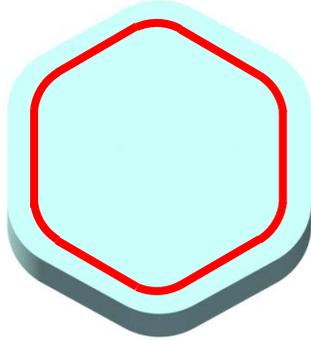


✓ High Q is obtained for circular cavity

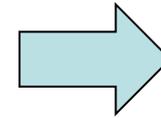
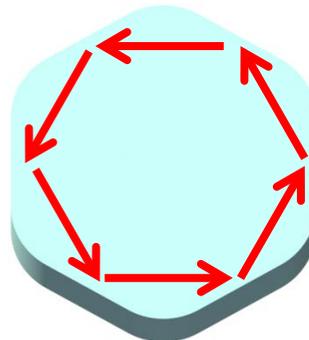
# Mode mixing between different modes in hexagonal cavities



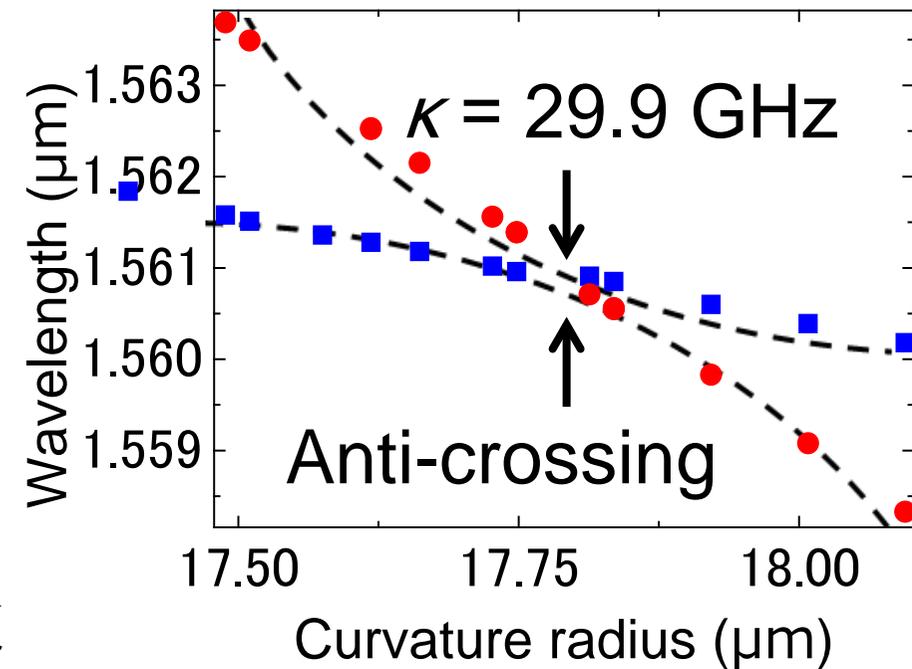
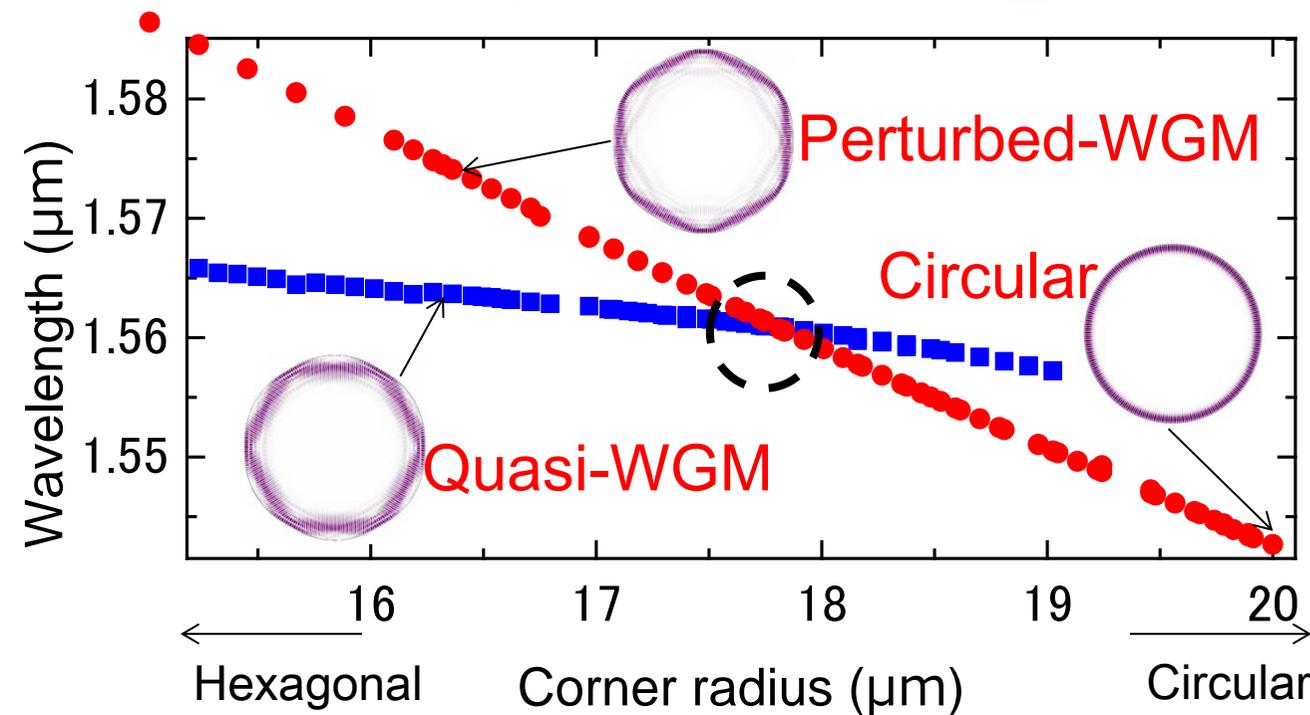
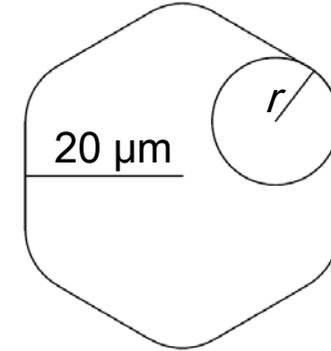
Perturbed - WGM



Quasi - WGM



FDTD model

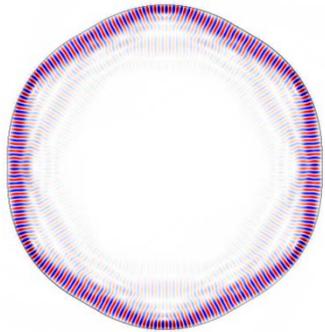


✓ Strong coupling occurs between perturbed & quasi modes

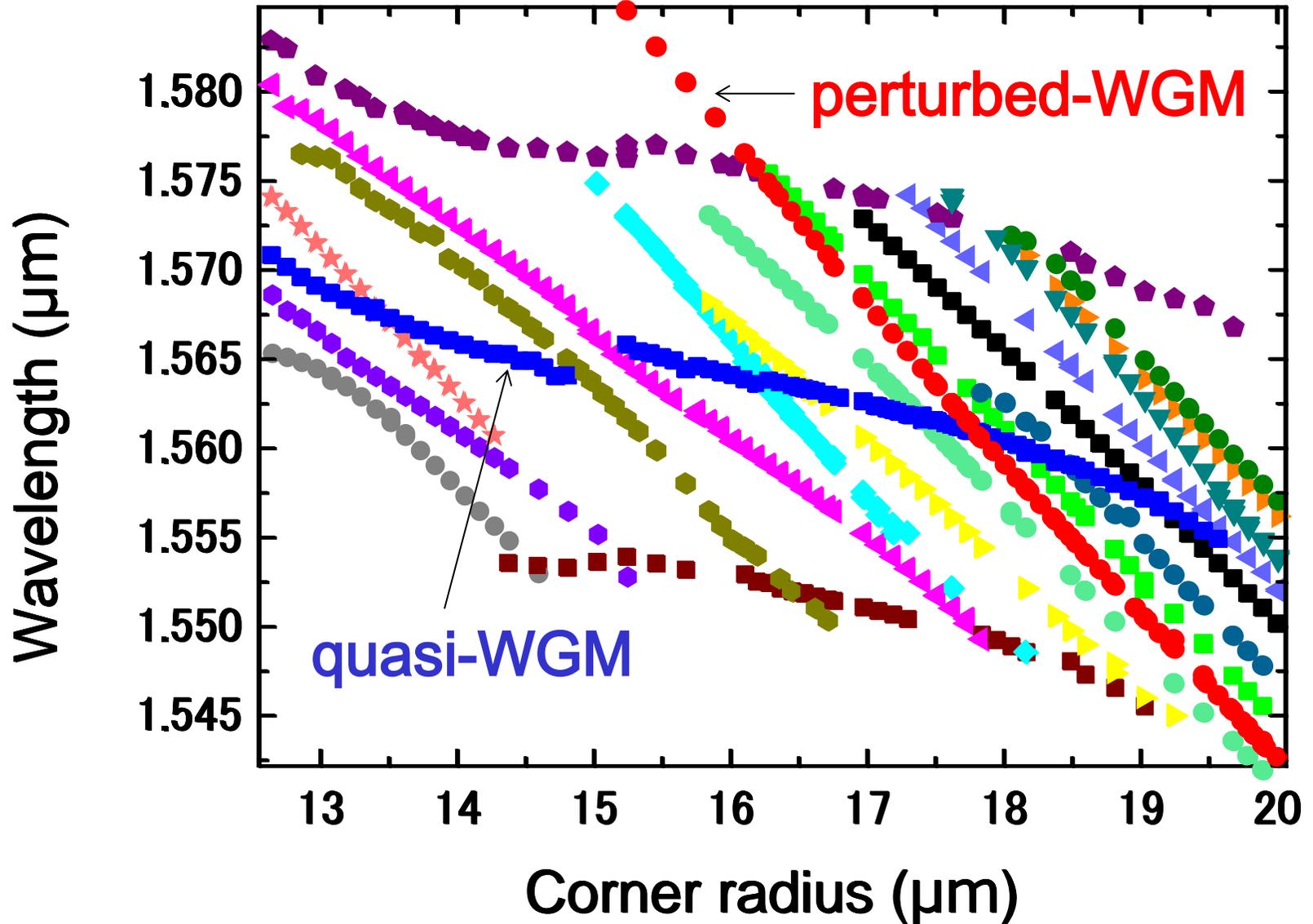
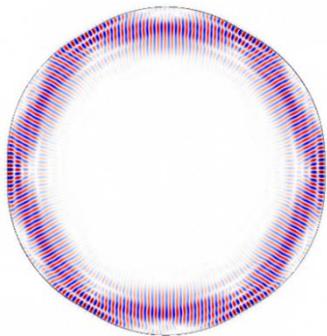
# Modes in hexagonal cavities (cont...)



**perturbed-WGM**



**quasi-WGM**

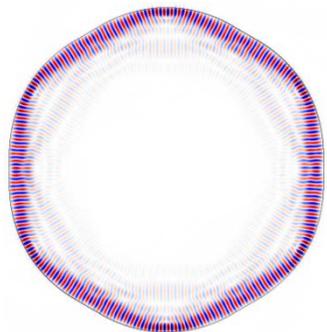


✓ A number of perturbed modes couple w/ quasi mode.

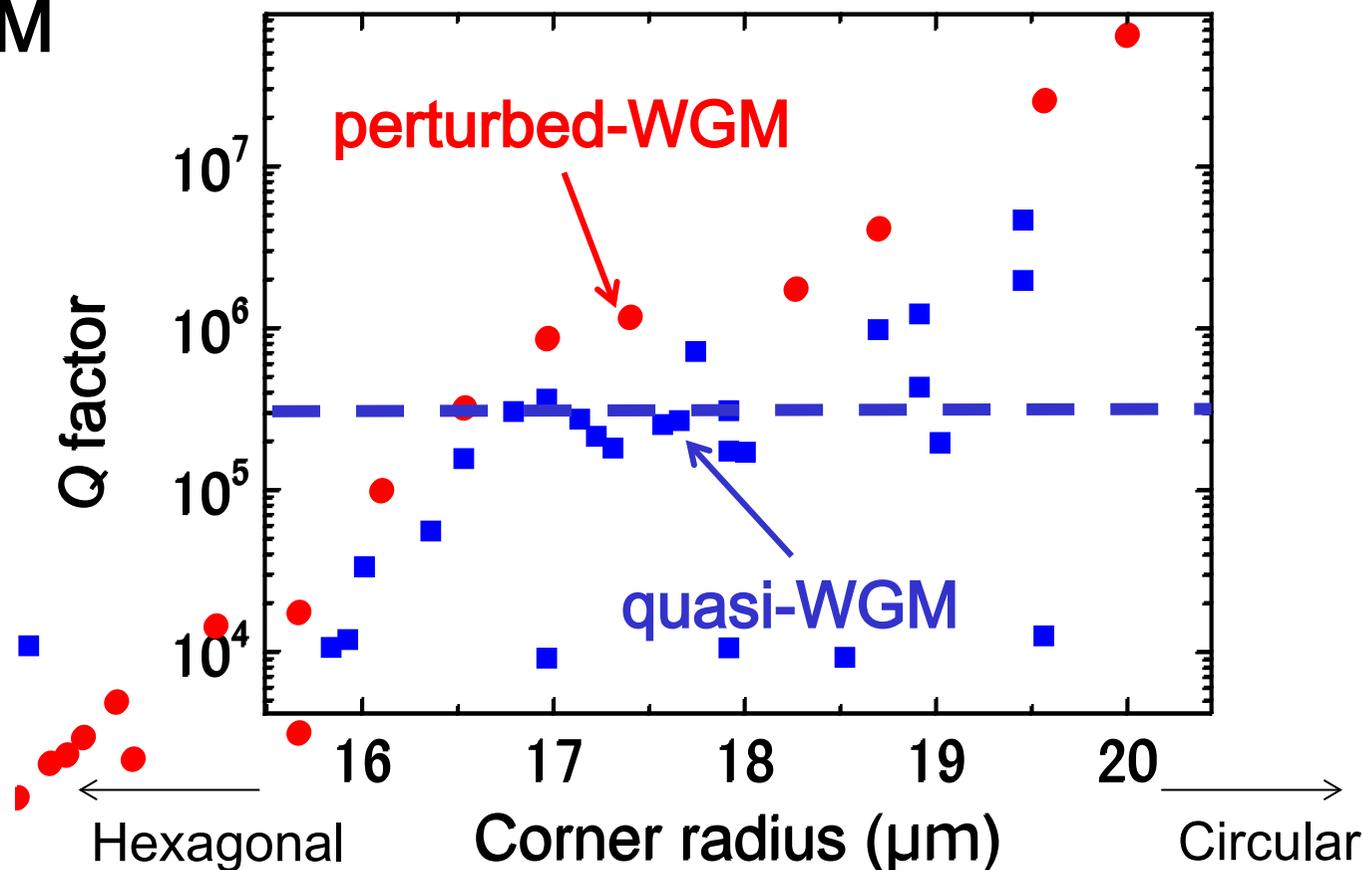
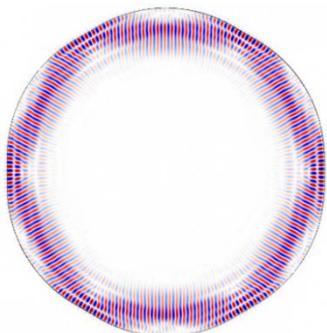
# Q factors for different WGM modes



**perturbed-WGM**



**quasi-WGM**



- ✓ Low Q = quasi-WGM (due to strong mode mixing)
- ✓ High Q = perturbed-WGM (but only w/ round corner)



## ① Fabricated crystalline WGM cavity by LHPG

- ✓  $Q = 1.6 \times 10^4$
- ✓  $V = 1.28 \times 10^{-2} \text{ mm}^3$

## ② Pre-heating allows the control of cross-sectional shape of the crystalline WGM cavity

## ③ Studied the effect of circle & hexagonal shape

- ✓ Mode coupling plays an important role to understand the low Q in quasi-WGM.
- ✓ High-Q is possible w/ perturbed-WGM when the corner is round.

# Acknowledgements



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文部科学省

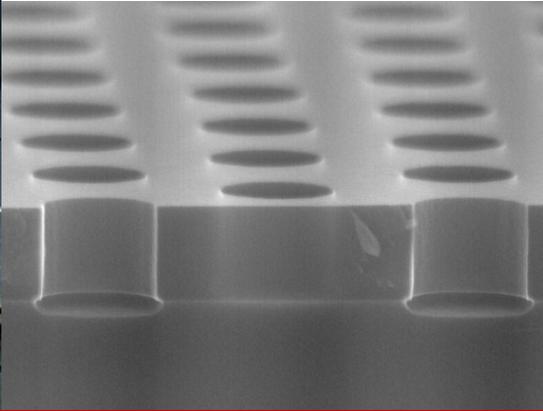
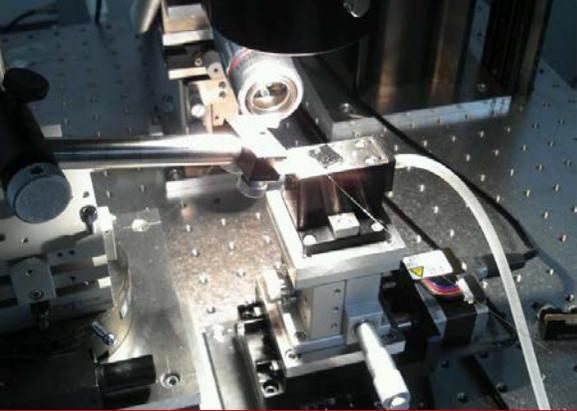
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Thank you very much.

# Improvement of $Q$



$$Q \text{ factor} \doteq \frac{3\lambda^3 a}{8n\pi^2 B^2 \sigma^2}$$

$\sigma$  : Root Mean Square (RMS)

$a$  : Radius of cavity

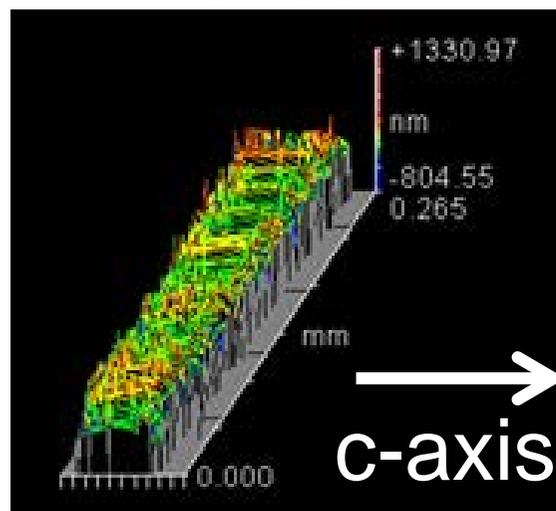
$\lambda$  : Wavelength

$B$  : Correlation length

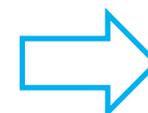
$n$  : Refractive index of material

$$Q = 1.6 \times 10^4$$

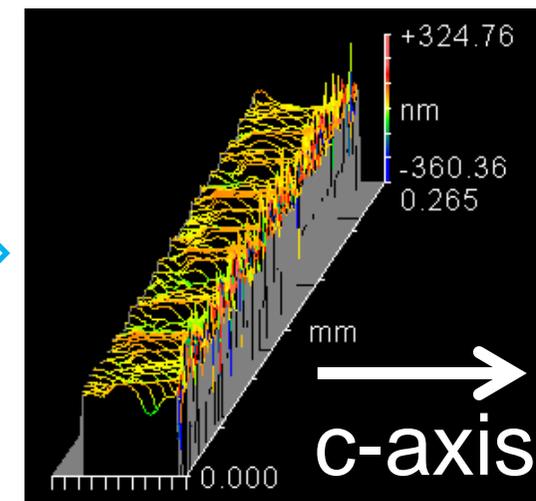
RMS: 65 nm



Pulling velocity  
12  $\mu\text{m/s}$



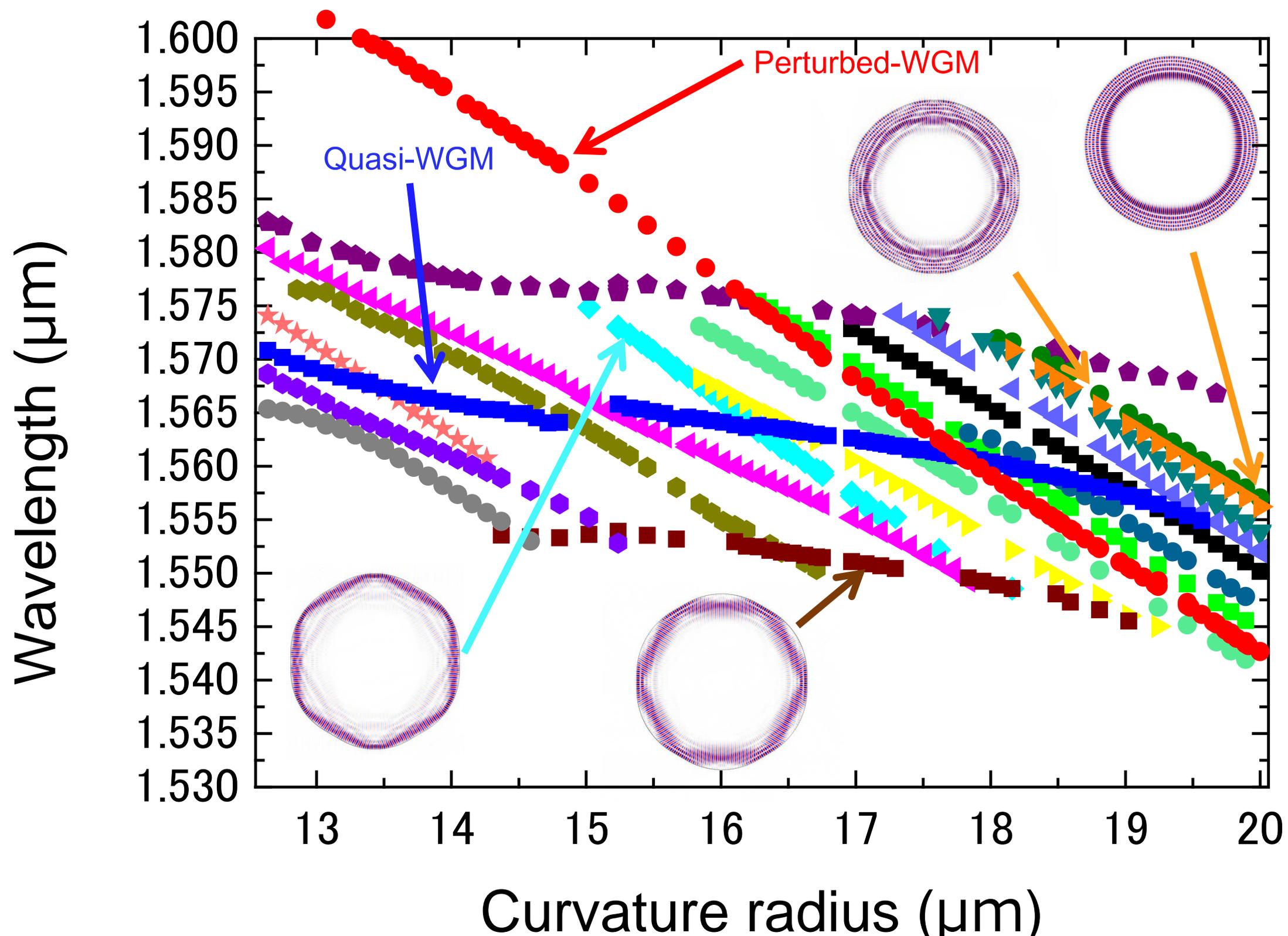
RMS: 6 nm



Pulling velocity  
2  $\mu\text{m/s}$

Can achieve higher  $Q$  factor by improve of surface roughness.

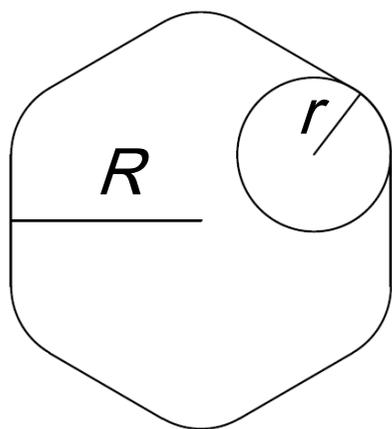
I. S. Grudin, *et al.*, Optics Communications 265, 33–38 (2006).



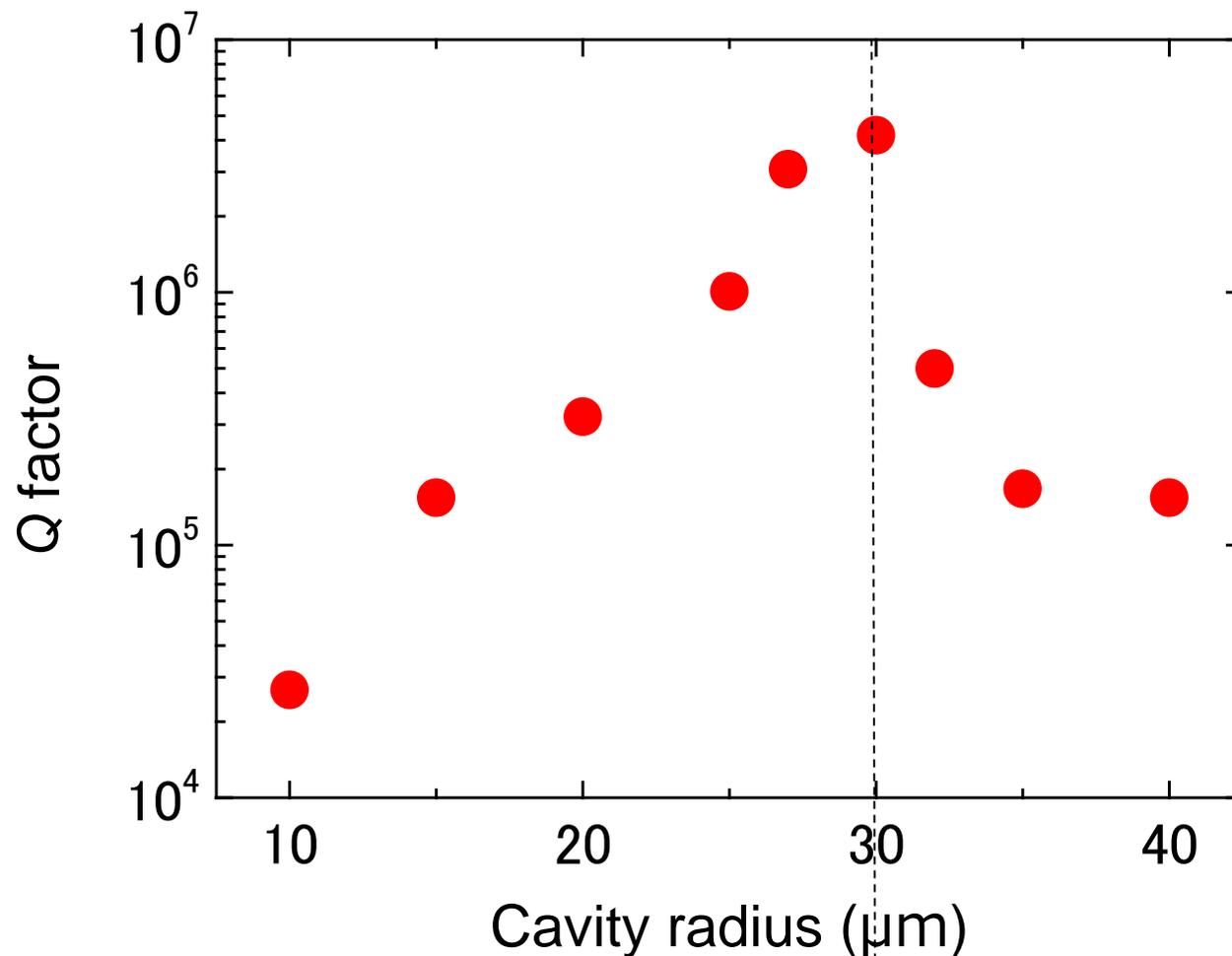
# Optimization of diameter



Calculation model



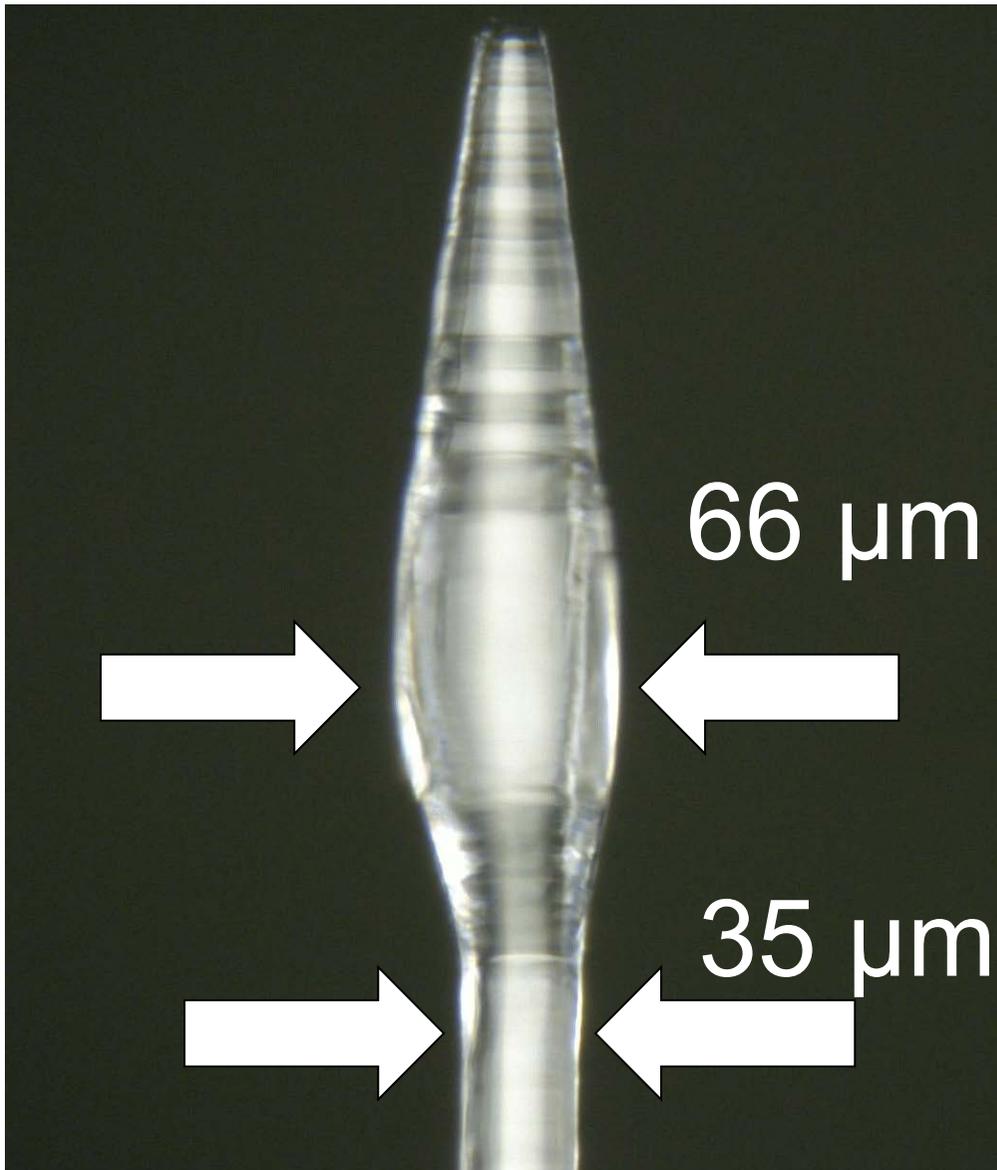
$$r = 0.8 \times R$$



← Total reflection condition | Mode coupling →

The optimal radius of the perturbed WGM is 30  $\mu\text{m}$ .

# Miniaturization of the fabricated rods



Using LHPG method, we can fabricate a sapphire rod with a diameter smaller than  $3\ \mu\text{m}$ .

R. S. Feigelson, W. L. Kway and R. K. Route, "Single Crystal Fibers by the Laser-Heated Pedestal Growth Method," SPIE **484**, 133 (1984).