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FTu5D.6

# **Broad-bandwidth pulse transmission through an ultrahigh-Q nanocavity with a chirped pulse**

**Zhelun Chen, Wataru Yoshiki, and Takasumi Tanabe\***

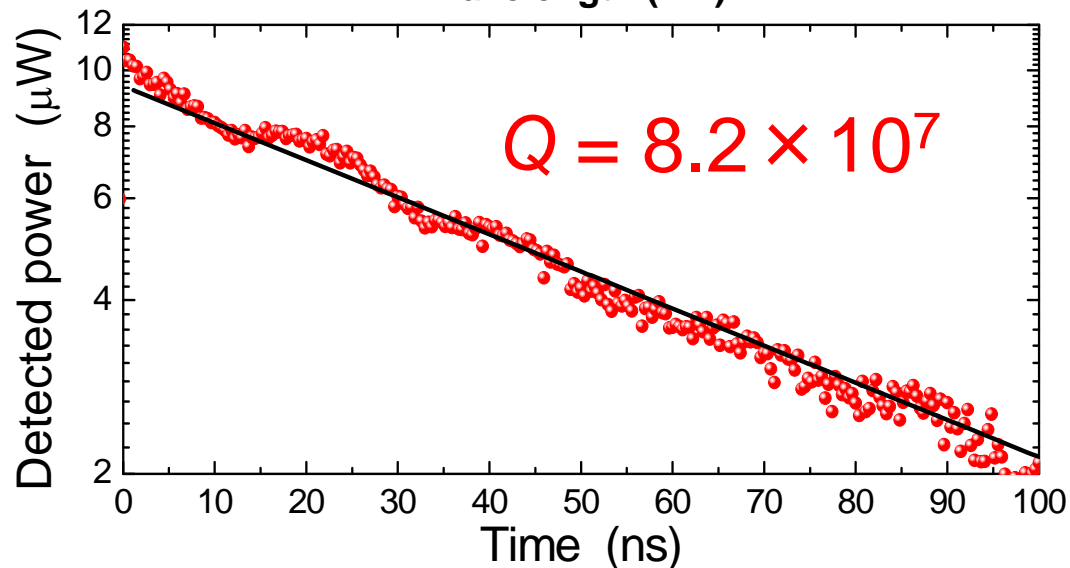
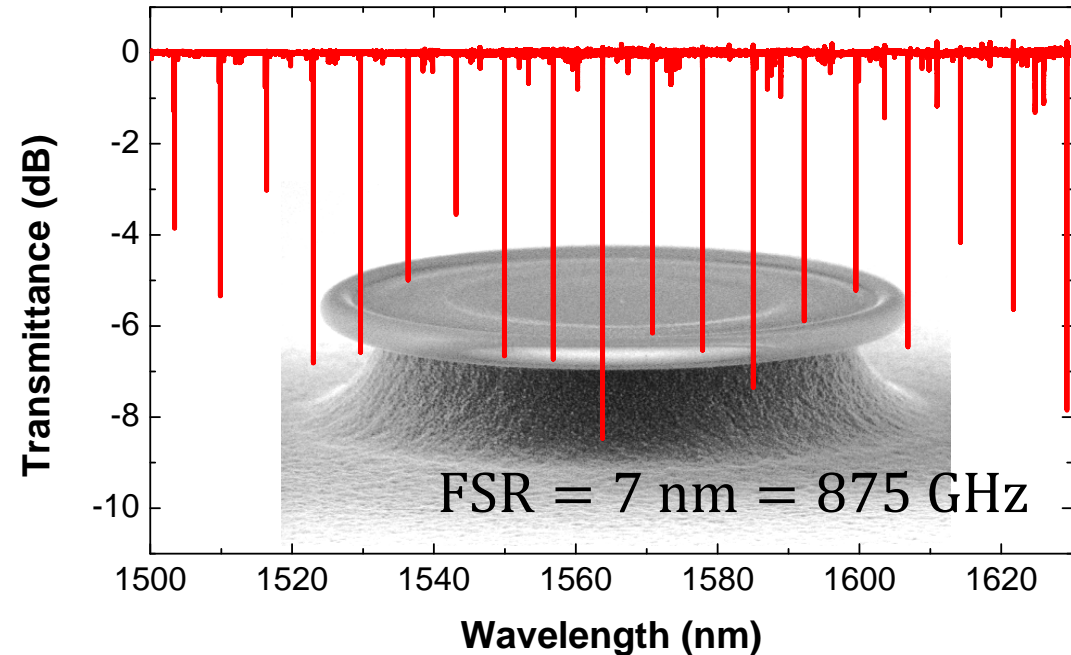
Department of Electronics and Electrical Engineering,  
Faculty of Science and Technology, Keio University

\*[takasumi@elec.keio.ac.jp](mailto:takasumi@elec.keio.ac.jp)

# Ultra-high Q microcavity



## ► Ultrahigh-Q microcavity



## ► Quality factor and mode volume

### ◆ Q-factor

$$Q = \omega \times \frac{\text{stored energy}}{\text{power in/out}}$$

### ◆ Photon density

$$\propto \frac{Q}{V}$$

## ► Applications

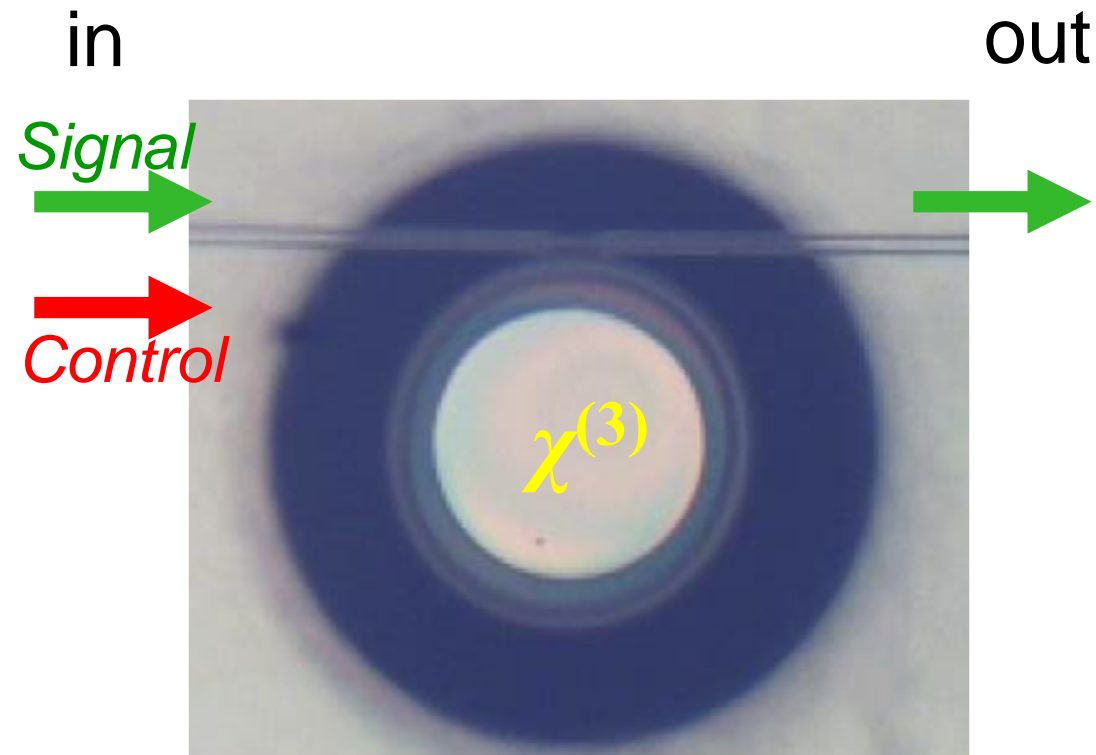
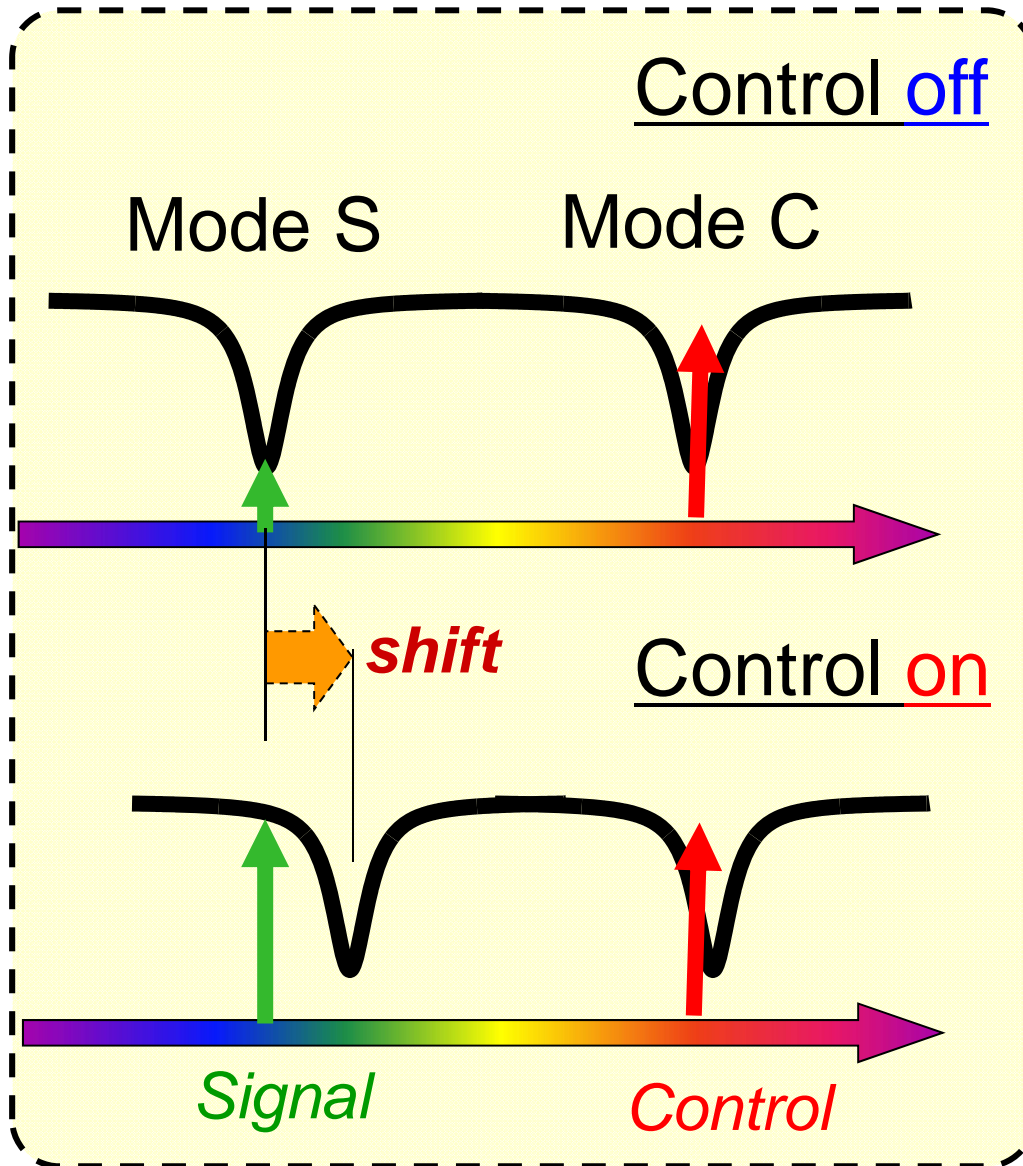
- All-optical switching
- Cavity QED devices
- Low-threshold lasers
- Optical sensors
- Optical frequency combs

# Optical switch in a microcavity: speed or power?



W. Yoshiki and T. Tanabe, Opt. Express **22**, 24332 (2014).

## ► Switching principle



Silica toroidal microcavity

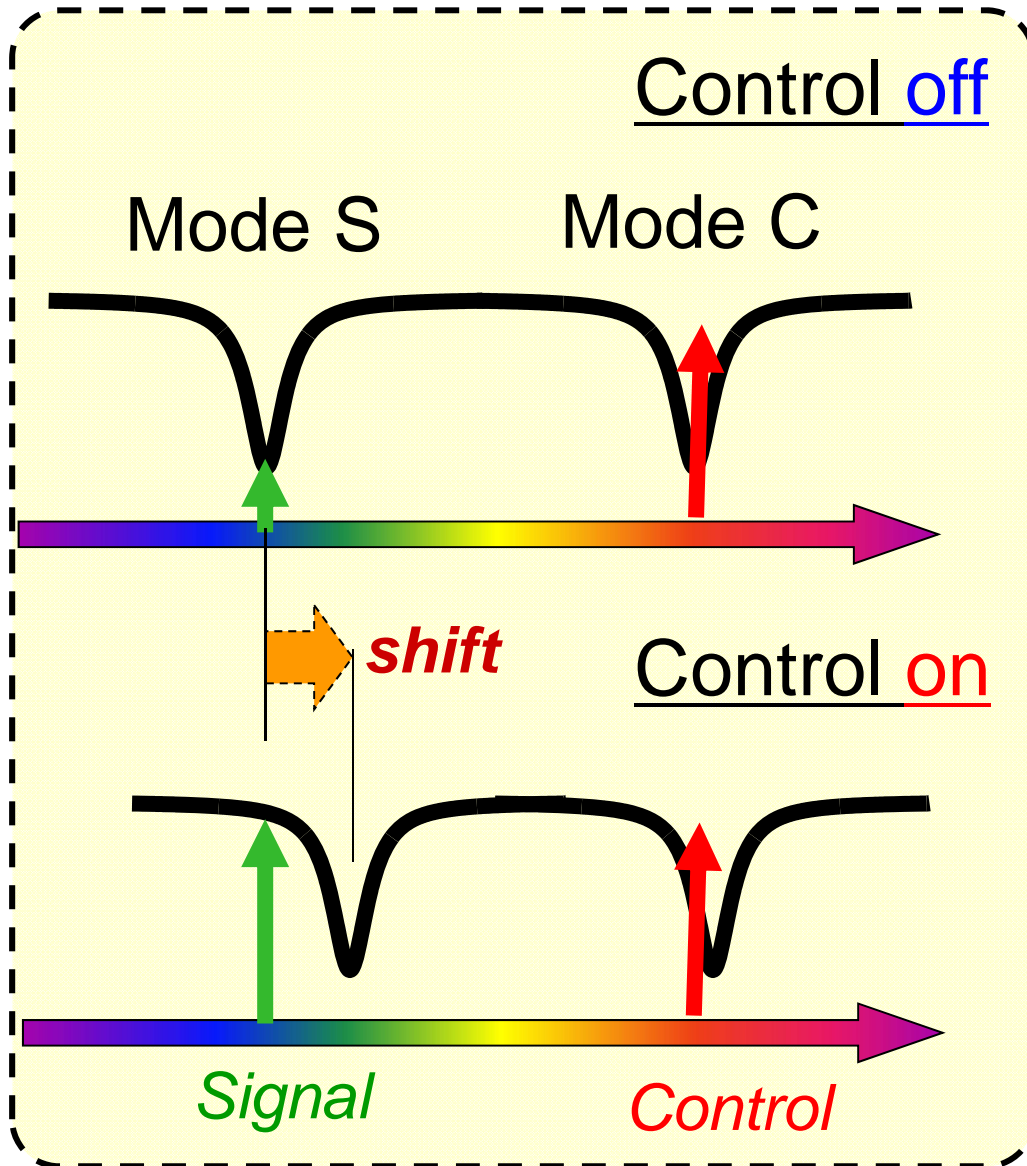


# Optical switch in a microcavity: speed or power?

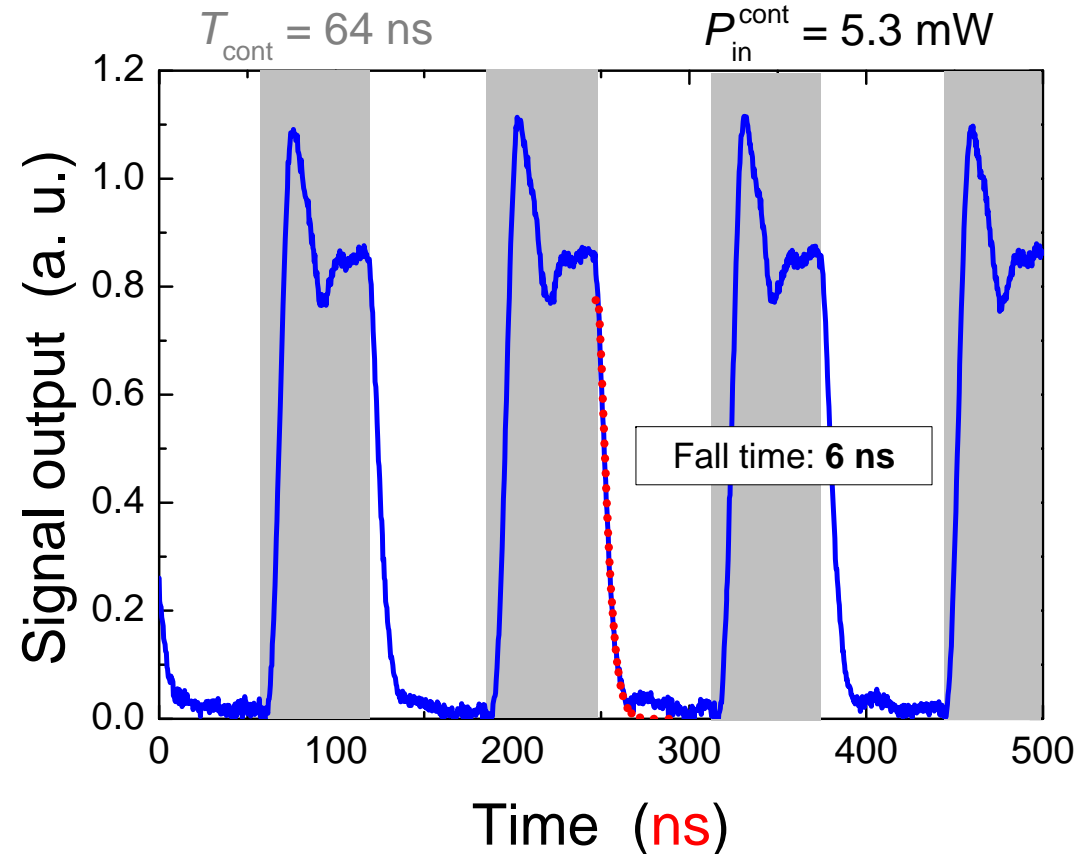


W. Yoshiki and T. Tanabe, Opt. Express **22**, 24332 (2014).

## ► Switching principle



## ► Low power Kerr switch

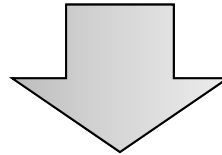


**Modulation observed at 36  $\mu\text{W}$**   
**Trade-off between Q and speed**



## Problems

❑ Trade-off between power and speed (high Q or low Q?)



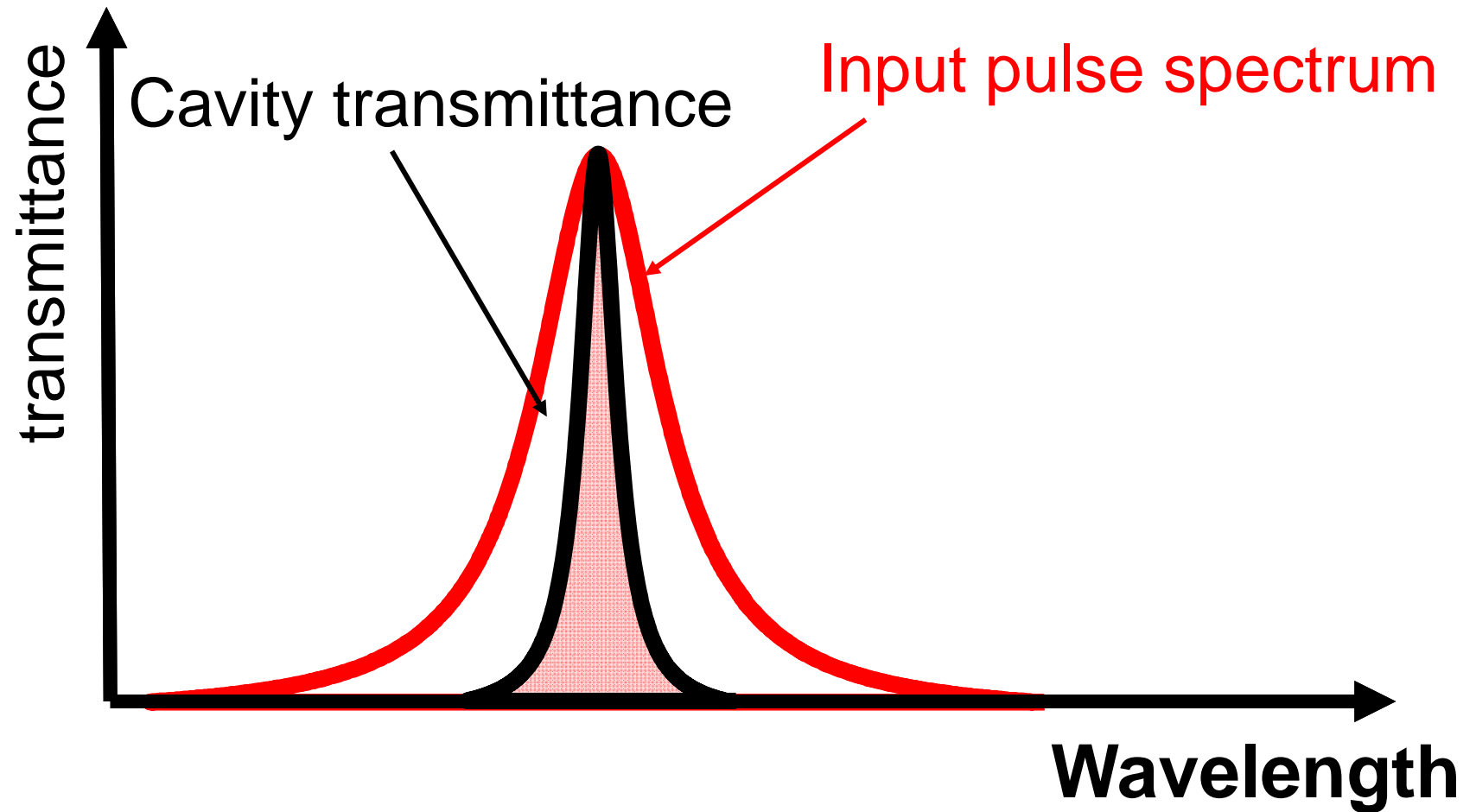
## Purpose of this study

❑ Transmit broad bandwidth pulse through high-Q nanocavity with simple scheme

# Basic idea – using self modulation of cavity



**w/o optical nonlinear effect**

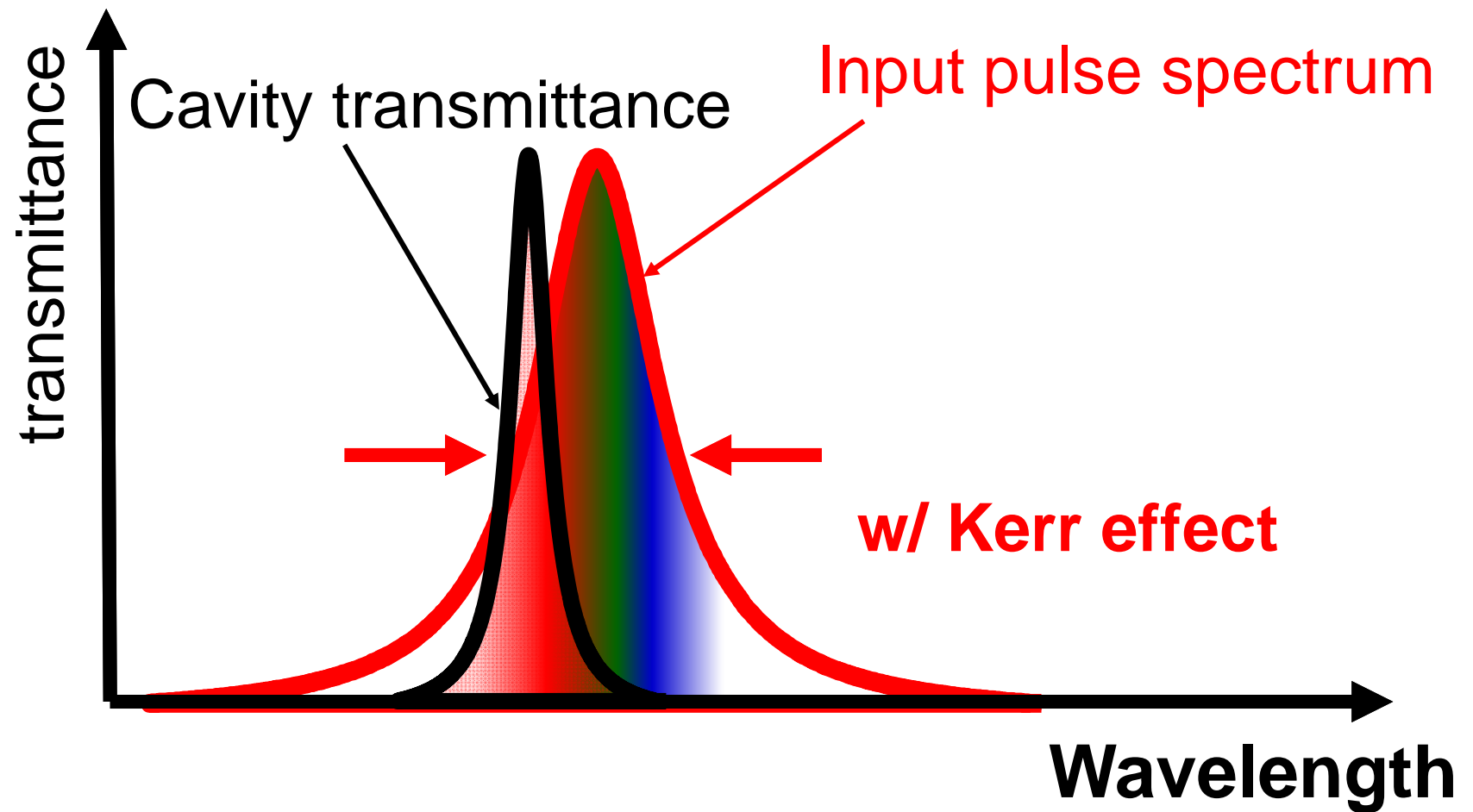


Only a portion of the pulse spectrum can transmit  
(i.e. narrow bandwidth)

# Basic idea – using self modulation of cavity



**w/ optical nonlinear effect**

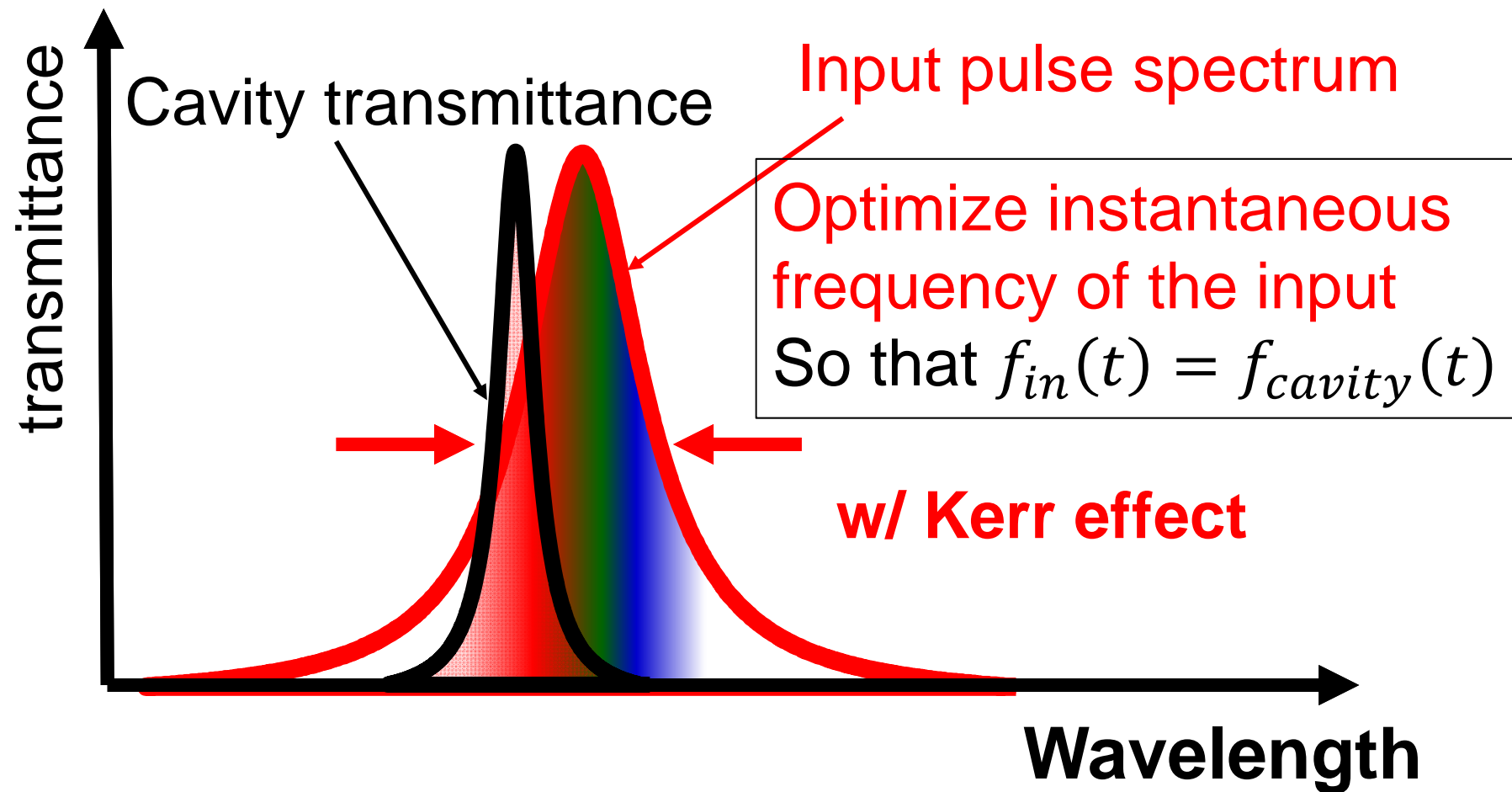


Broad bandwidth pulse can transmit ultrahigh Q cavity

# Basic idea – using self modulation of cavity



## w/ optical nonlinear effect



Broad bandwidth pulse can transmit ultrahigh Q cavity



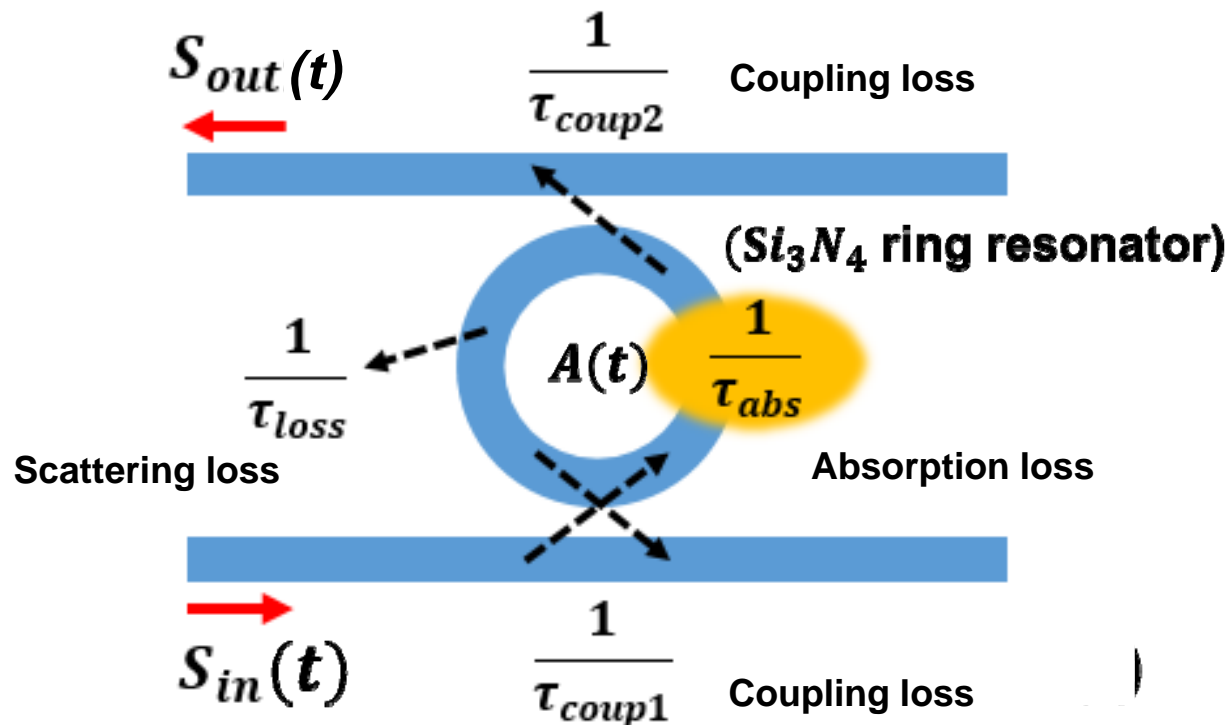
# Model – Add-drop system & CMT



## Coupled mode theory (CMT)

$$\frac{dA(t)}{dt} = \left[ j2\pi c \left( \frac{1}{\lambda_r + \delta\lambda(t)} - \frac{1}{\lambda_{in}} \right) - \frac{1}{2} \left( \frac{1}{\tau_{loss}} + \frac{1}{\tau_{abs}} + \frac{1}{\tau_{coup1}} + \frac{1}{\tau_{coup2}} \right) \right] A(t) + \sqrt{\frac{1}{\tau_{coup1}}} \exp(j\theta) S_{in}(t)$$

### □ Add-drop system



$A(t)$ : Cavity mode amplitude  
 $\lambda_0$ : Resonant wavelength (cold cavity)  
 $\delta\lambda(t)$ : Resonance wavelength shift  
 $\lambda_{in}$ : Input wavelength  
 $\theta$ : Phase difference

**Analyze  $S_{out}(t)$   
in Add-drop system by CMT**

# Optimized spectrum phase & detuning

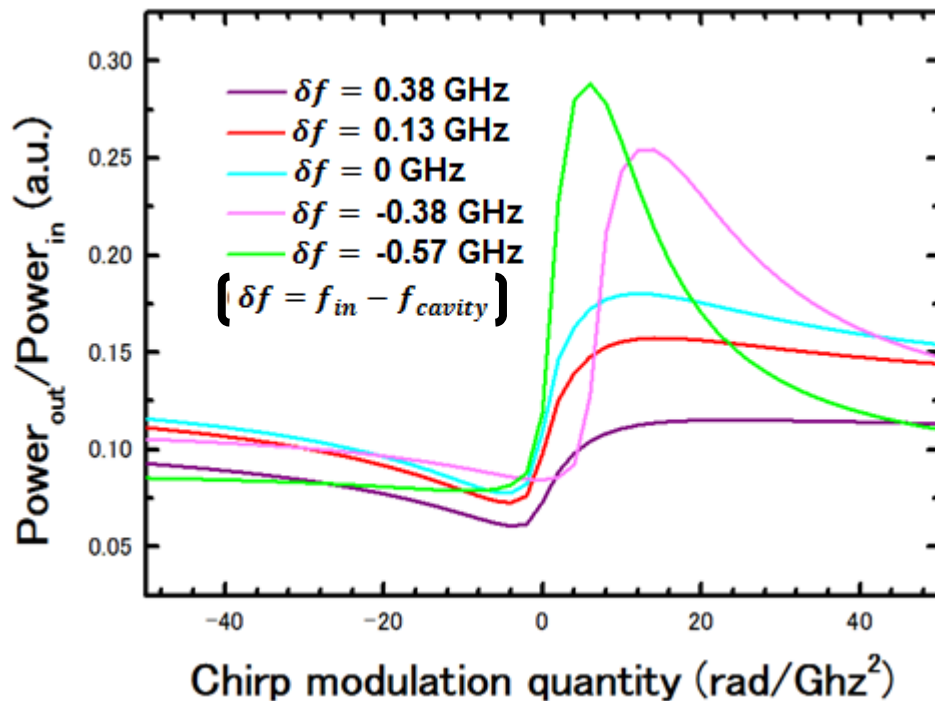


Input energy: 28.4 pJ

FTL pulse width: 0.45 ns (1.2 GHz)

$Q = 7.5 \times 10^5$

( $T \sim 11\%$  w/ TL input)



28% of input energy can be transported through cavity  
(**2.4 times greater** than that of FTL pulse)

# Optimized spectrum phase & detuning

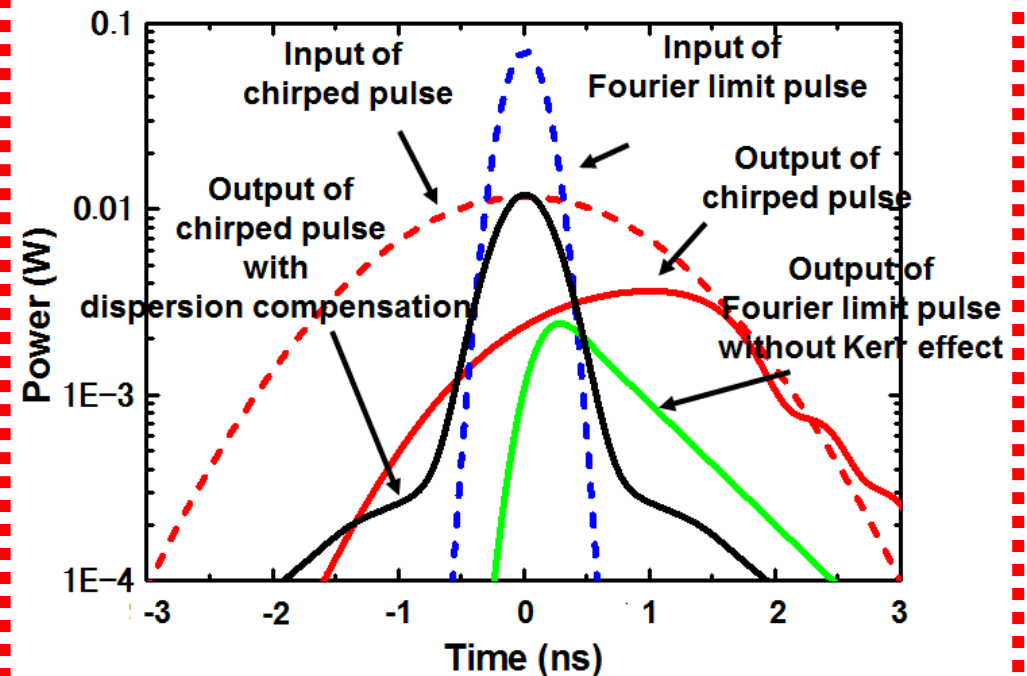
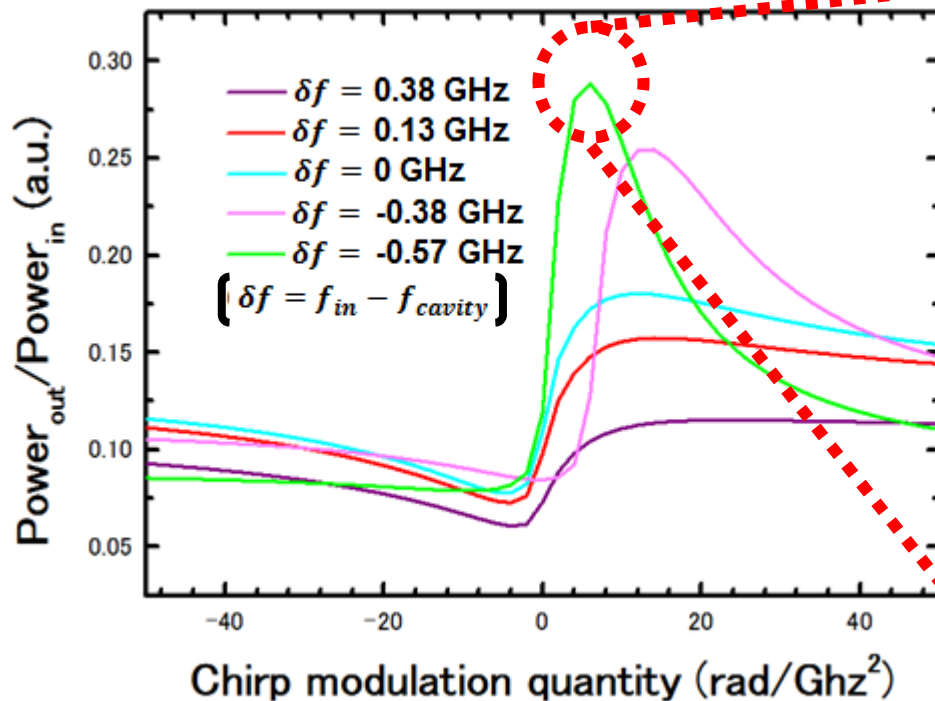


Input energy: 28.4 pJ

$$Q = 7.5 \times 10^5$$

FTL pulse width: 0.45 ns (1.2 GHz)

( $T \sim 11\%$  w/o Kerr)

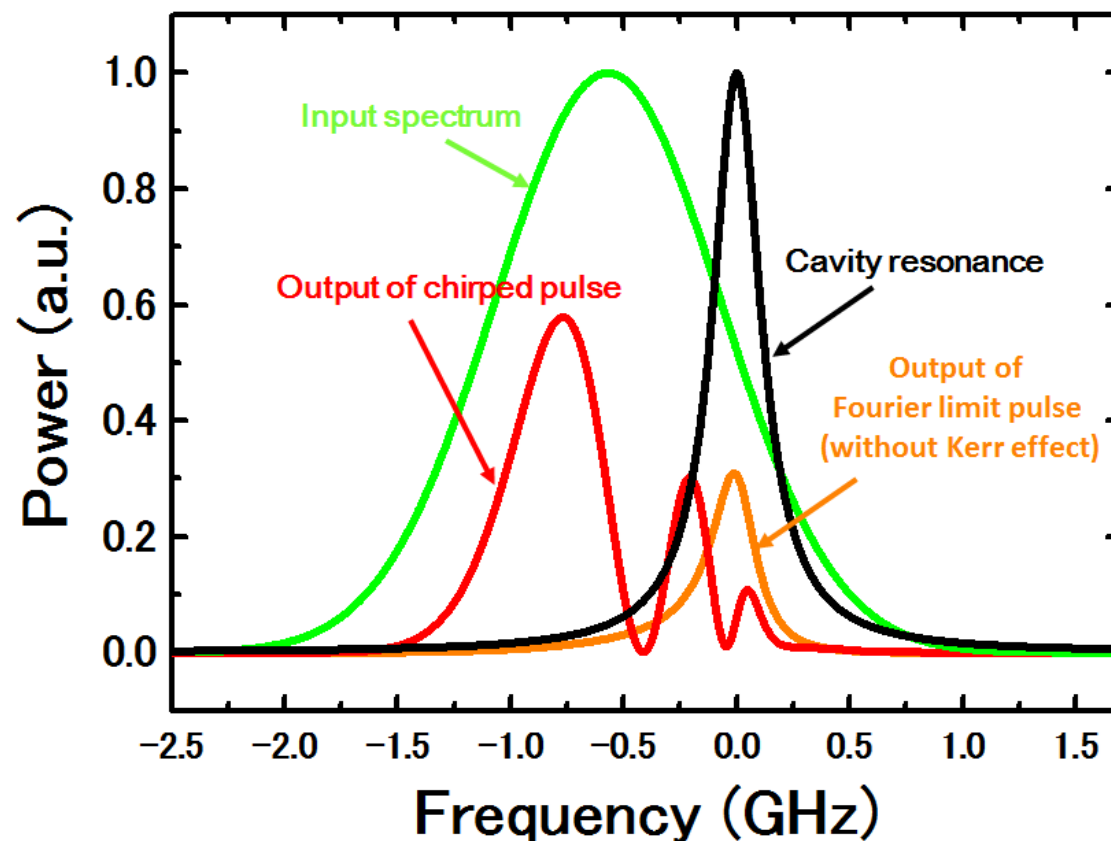


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# Discussion



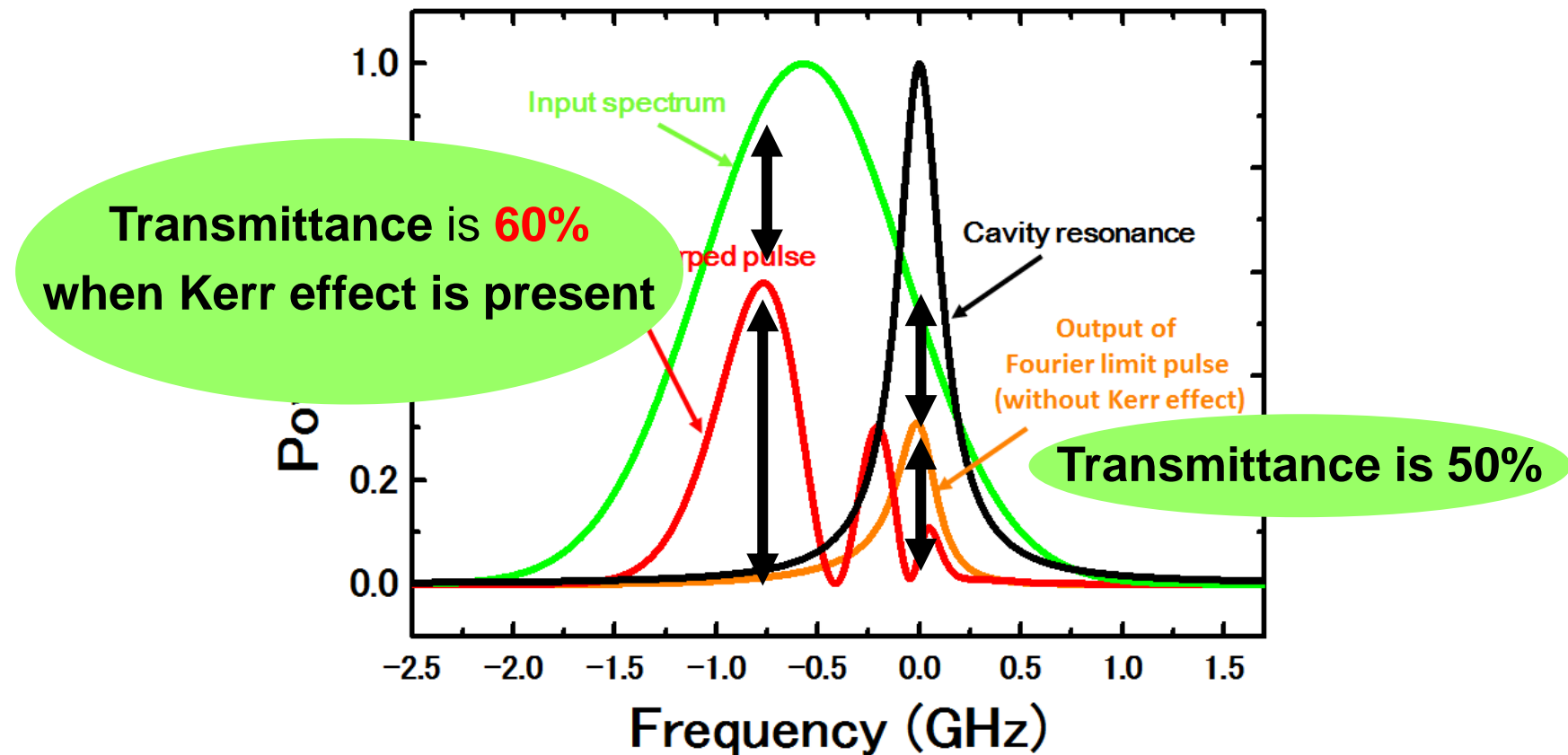
(Quantity of second spectrum phase:  $4.5 \text{ rad/GHz}^2$ ,  
Resonance frequency (cool cavity):  $194 \text{ THz}$ ,  $\delta f = -0.57 \text{ GHz}$ )



# Discussion



(Quantity of second spectrum phase:  $4.5 \text{ rad/GHz}^2$ ,  
Resonance frequency (cool cavity):  $194 \text{ THz}$ ,  $\delta f = -0.57 \text{ GHz}$ )



- Why high transmittance ?

# Classic (adiabatic) wavelength tuning of light



T. Tanabe, *et al.*, Phys. Rev. Lett. **102**, 043907 (2009)

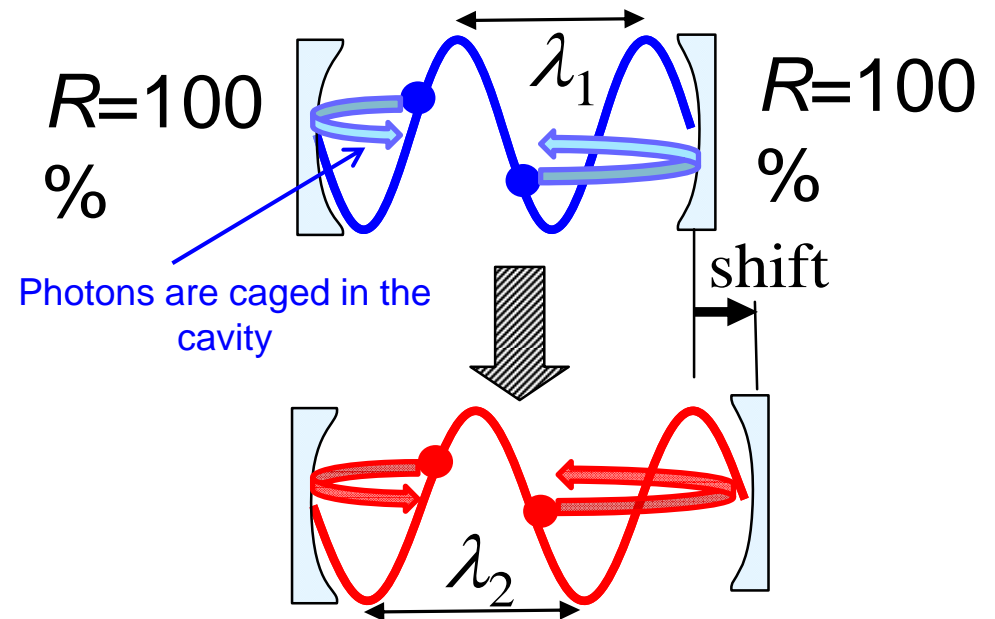
## ■ Classical frequency tuning: Case of tone (ex: guitar string)



**Q:** How can we change the pitch when the string is already plucked?

**A:** By **changing the tension** of the string. But it must be done before the tone disappears.

## ■ Classical frequency tuning: Case of light (ex: high-Q cavity)

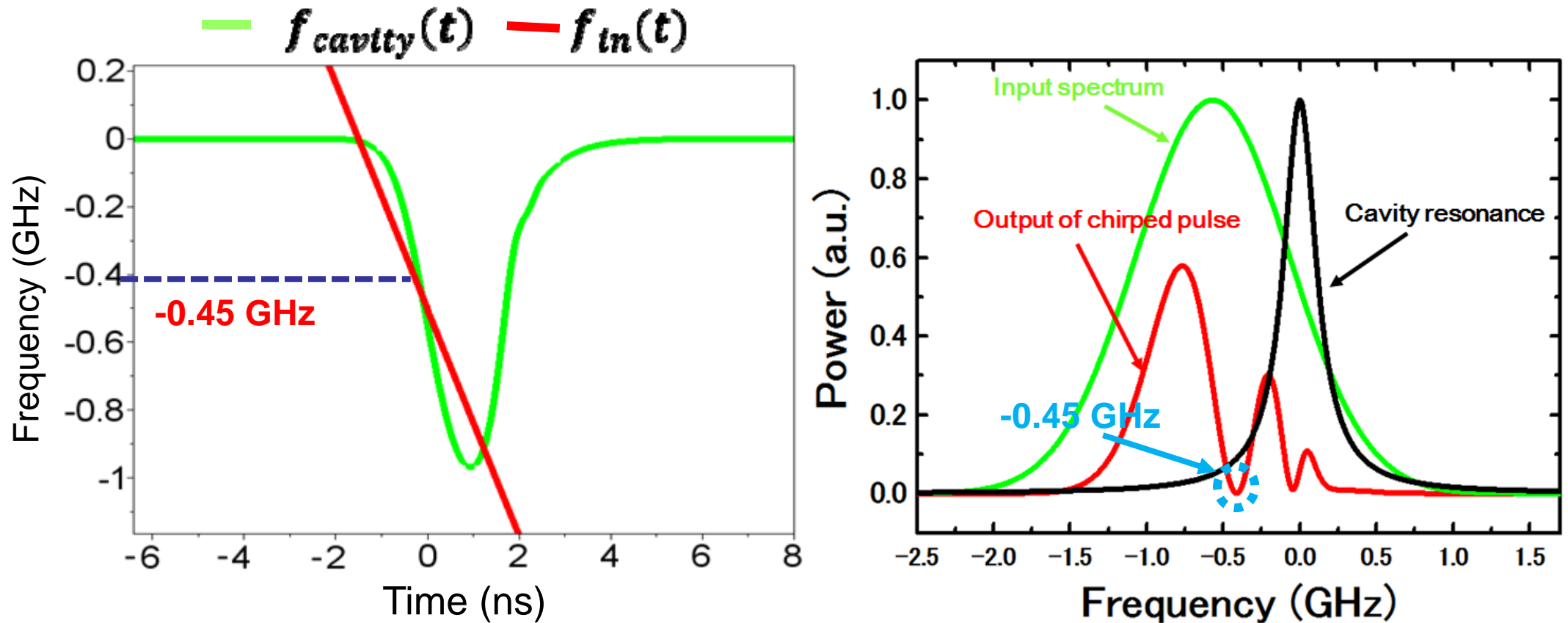


**Q:** What will happen when we **change the cavity length**, when the mirror is perfect and the light cannot escape?

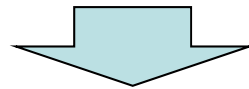
**A:** The frequency of the light will follow the cavity resonance adiabatically!



# Analysis of adiabatic wavelength conversion



Speed of the cavity resonance shift is the highest at -0.45 GHz



frequency component at -0.45 GHz changes their wavelength and then output as a low frequency light



□ Obtained optimized linear chirp to permit broad-bandwidth transmittance

- 28% of input energy can transmit
- **2.4 times greater** than inputting FTL pulse

□ Showed adiabatic wavelength conversion plays an important role in this event