

ALPS5-I1-7

Nonlinear Parametric Oscillation Phase-matched via High-order Dispersion in High-Q Silica Toroid Microresonators

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Outline

1. Background

- Optical parametric oscillator
- Phase-matched four-wave mixing in microresonators

2. Numerical simulation of cavity dispersion

3. Experimental observation

4. Summary



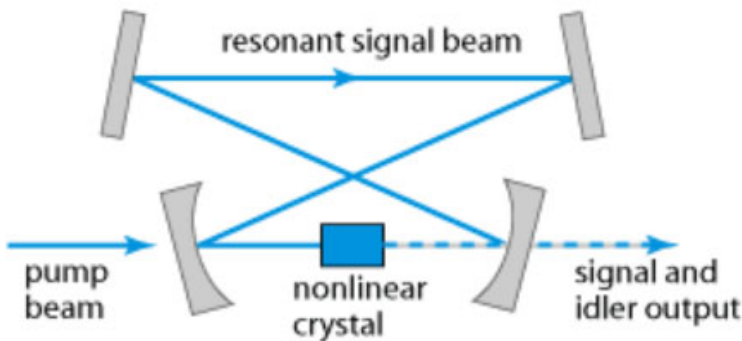
Optical parametric oscillators (OPOs)

$\chi^{(2)}$ Nonlinear crystal

Difference frequency generation



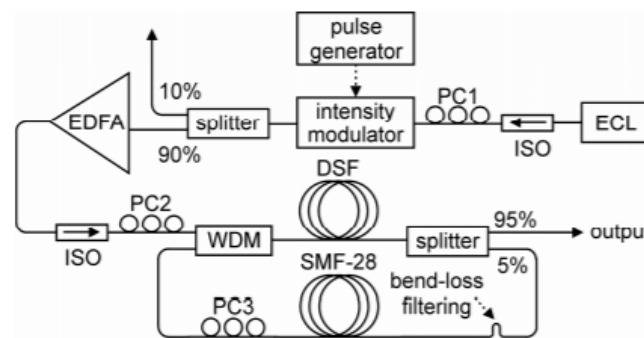
N. Savage, Nat. Photonics **4**, 124 (2010).



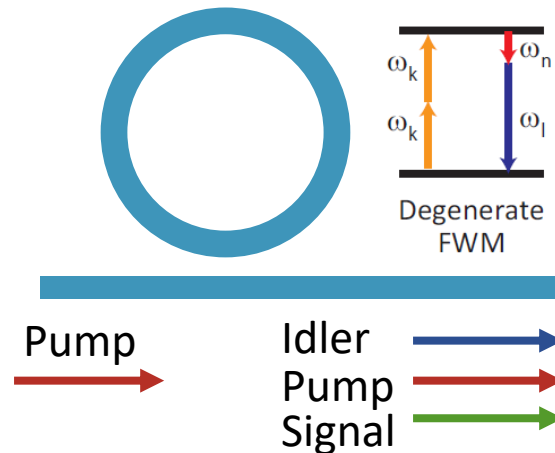
RP Photonics

$\chi^{(3)}$ Optical fiber OPO

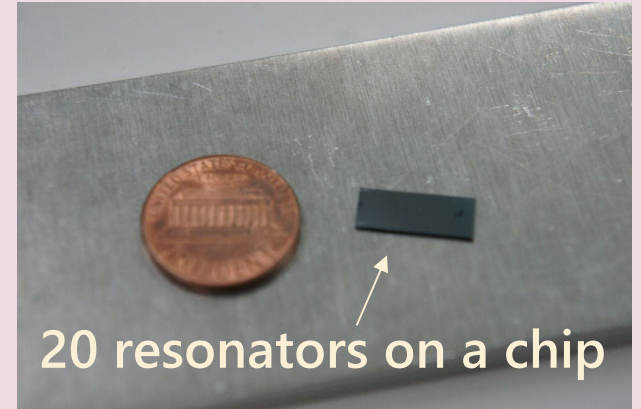
Degenerated FWM



G. K. L. Wong, et al. Opt. Express **15**, 2947 (2007).



High-Q Microresonators



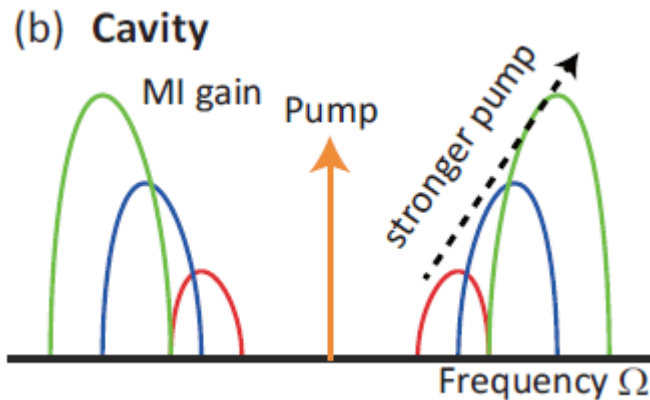
20 resonators on a chip

- ✓ On chip-scale (small)
- ✓ Low cost
- ✓ Low-power drive

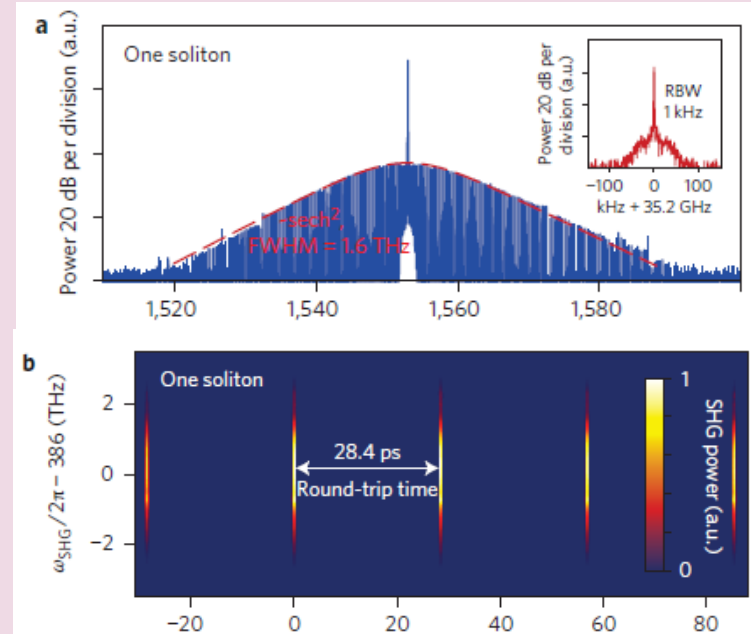
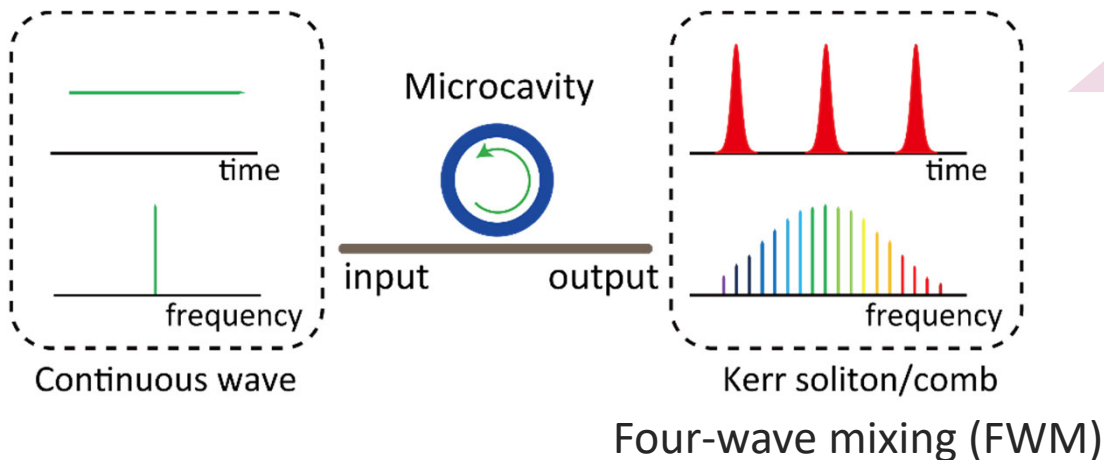


Phase-matched FWM in microresonators

❖ Anomalous dispersion Kerr comb generation



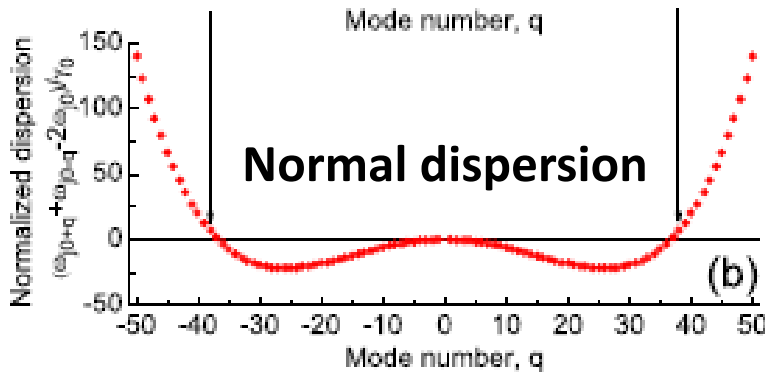
- ✓ Initial FWM requires modulation instability gain
- ✓ MI gain requires *anomalous dispersion*
- ✓ Balance between Kerr effect and dispersion





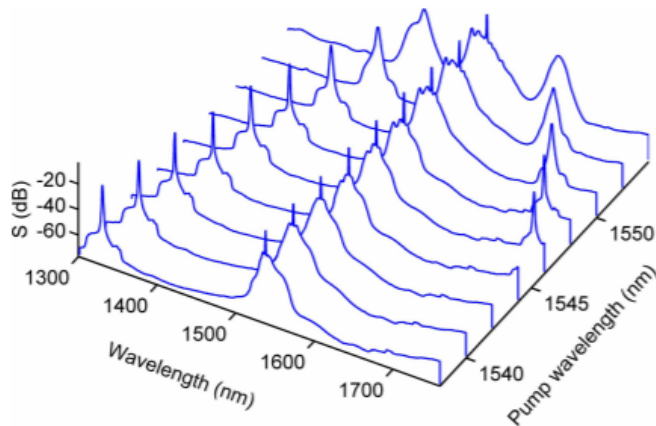
Phase-matched FWM in microresonators

❖ Scheme in this work (Parametric sideband generation)

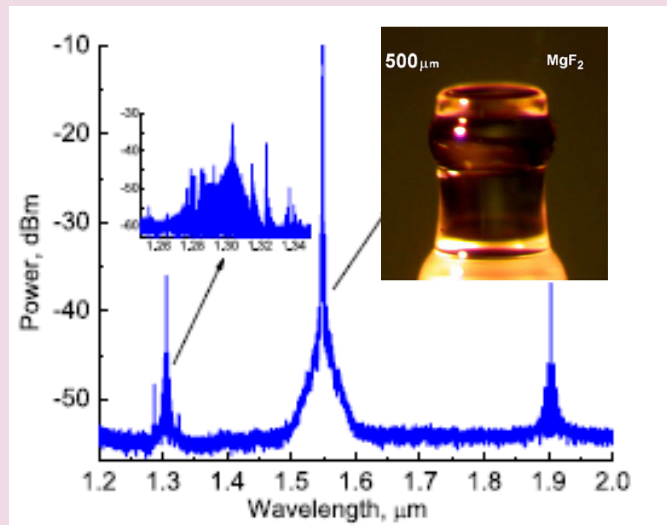


- ✓ MI gain is achieved by unique phase-matching
- ✓ Dispersion near the pump is normal
- ✓ **Phase-matching far from the pump mode**

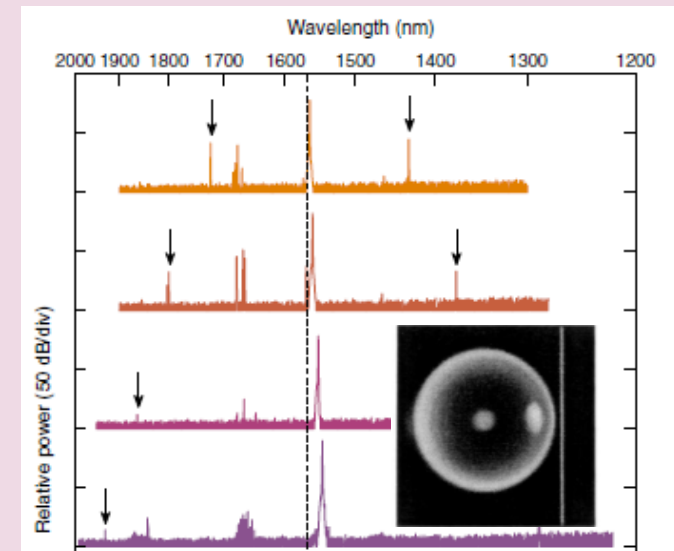
Optical fiber OPO



Bulk magnesium fluoride

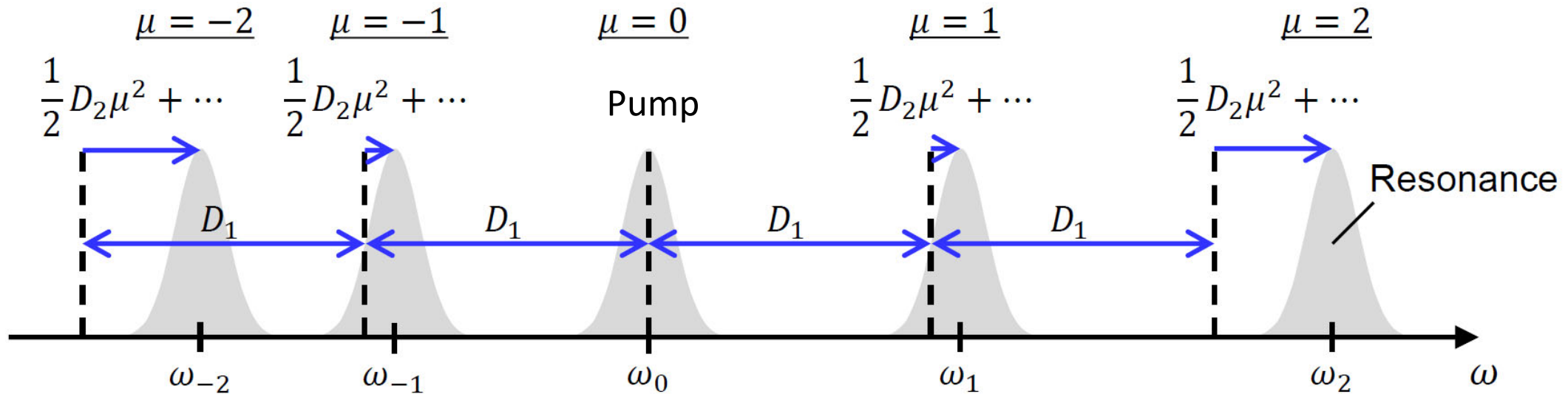


Silica microspheres





Definition of cavity dispersion



Resonance frequencies (μ is mode number)

$$\omega_\mu = \omega_0 + D_1\mu + \frac{1}{2}D_2\mu^2 + \frac{1}{6}D_3\mu^3 + \frac{1}{24}D_4\mu^4$$

Total dispersion

$D_2 > 0$: Anomalous dispersion

$D_2 < 0$: Normal dispersion

Phase-matching condition (residual dispersion) for initial sidebands

$$\Delta\omega = \omega_\mu - \omega_0 - (\omega_0 - \omega_{-\mu}) = D_2\mu^2 + \frac{D_4}{12}\mu^4 \rightarrow 0 \quad \mu^2 = -\frac{12D_2}{D_4} \quad (D_2 \cdot D_4 < 0)$$

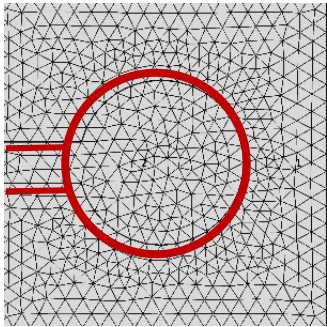
Fourth-order dispersion plays important role in phase-matched FWM!



Calculation method of cavity dispersion

Geometry dispersion

Finite-element method



Resonance frequency (Hz)

COMSOL Sellmeier equation

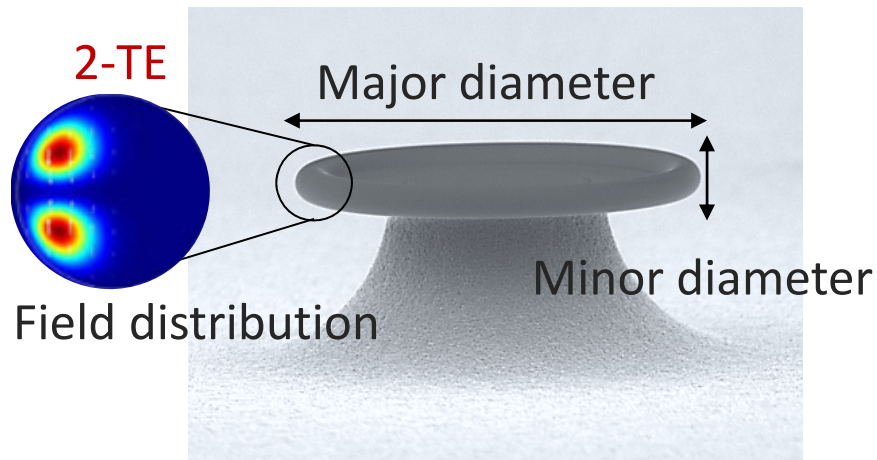
Refractive index

Material dispersion

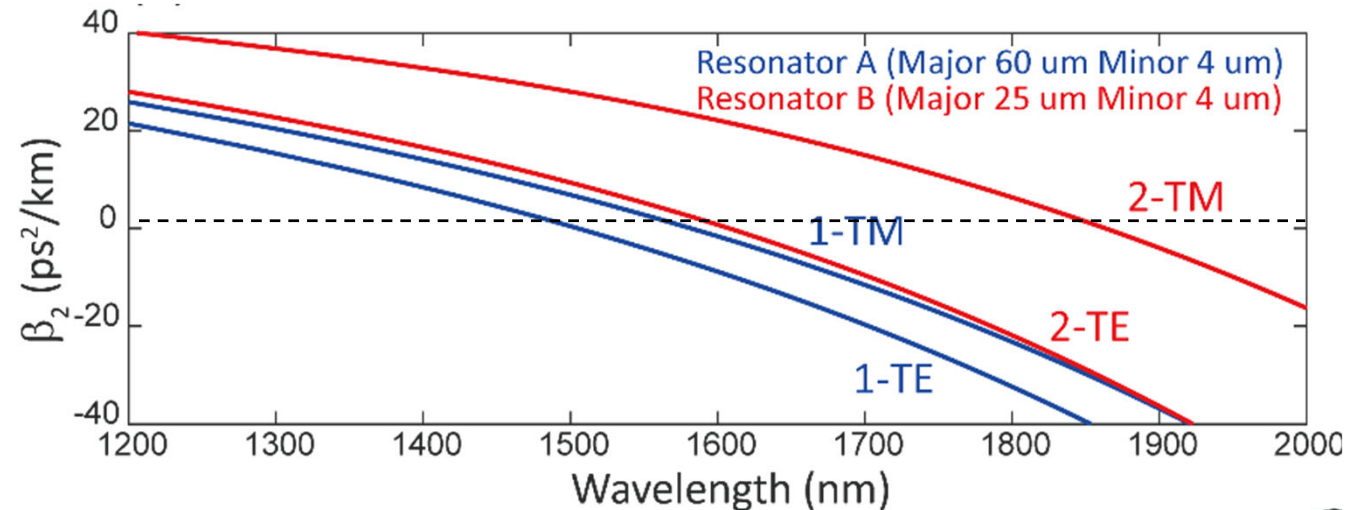
$$n^2 = 1 + \sum_i \frac{A_i \cdot \lambda^2}{\lambda^2 - B_i^2}$$

A, B : coefficient (const.)

Silica toroid microresonator



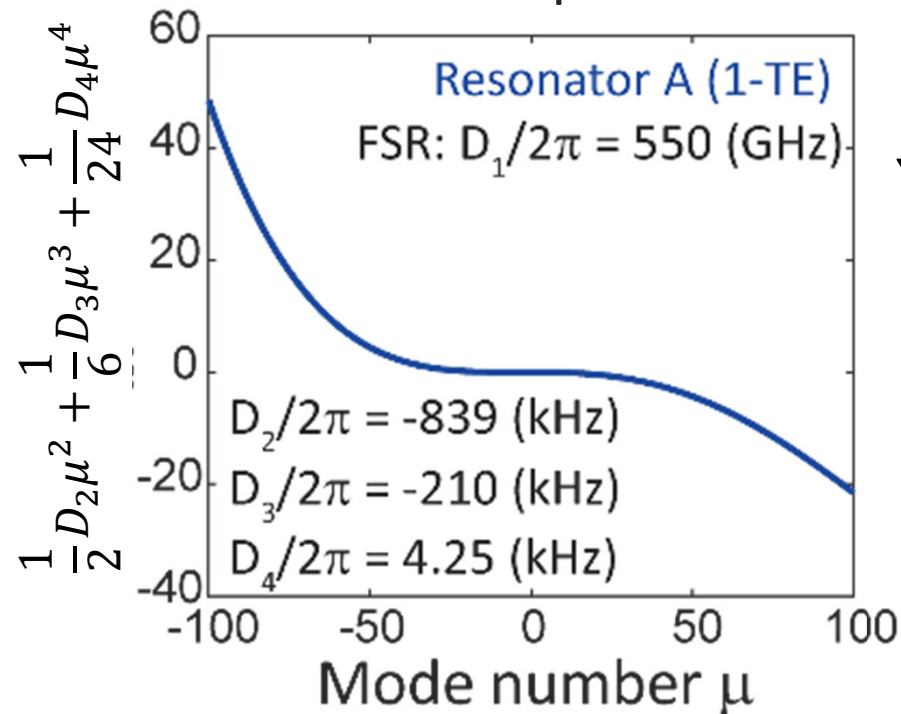
Group velocity dispersion



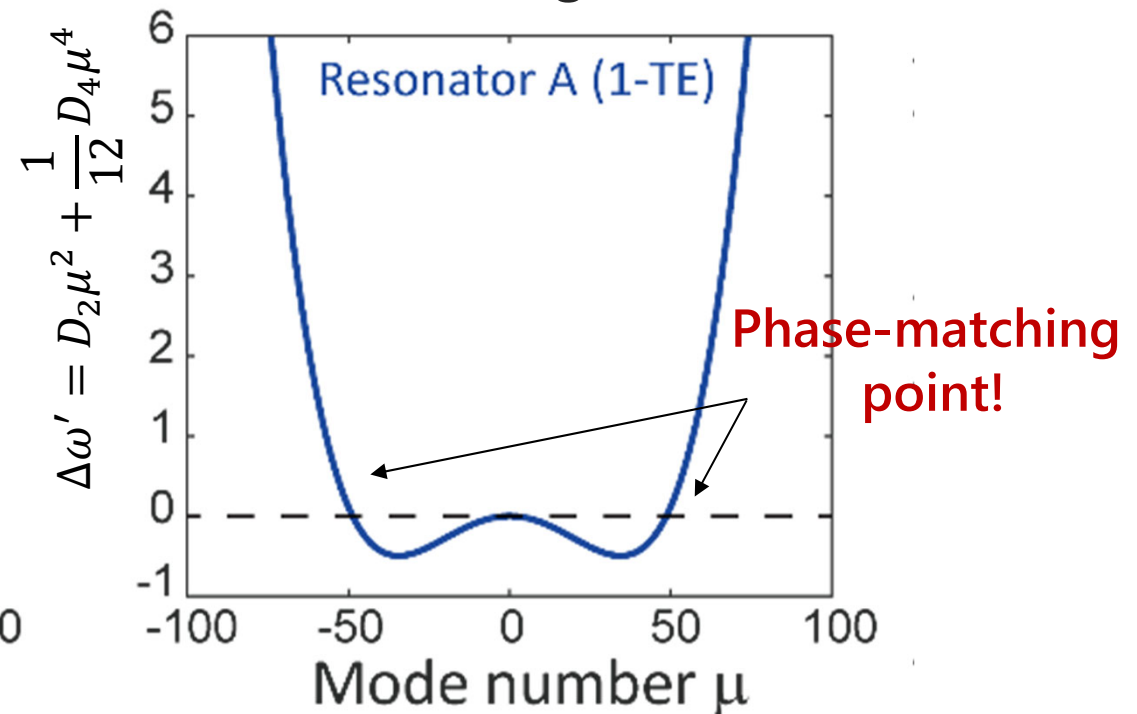
Phase-matching points depending on cavity geometry

Major diameter 120 μm , Minor diameter 8 μm , 1-TE mode

Total dispersion

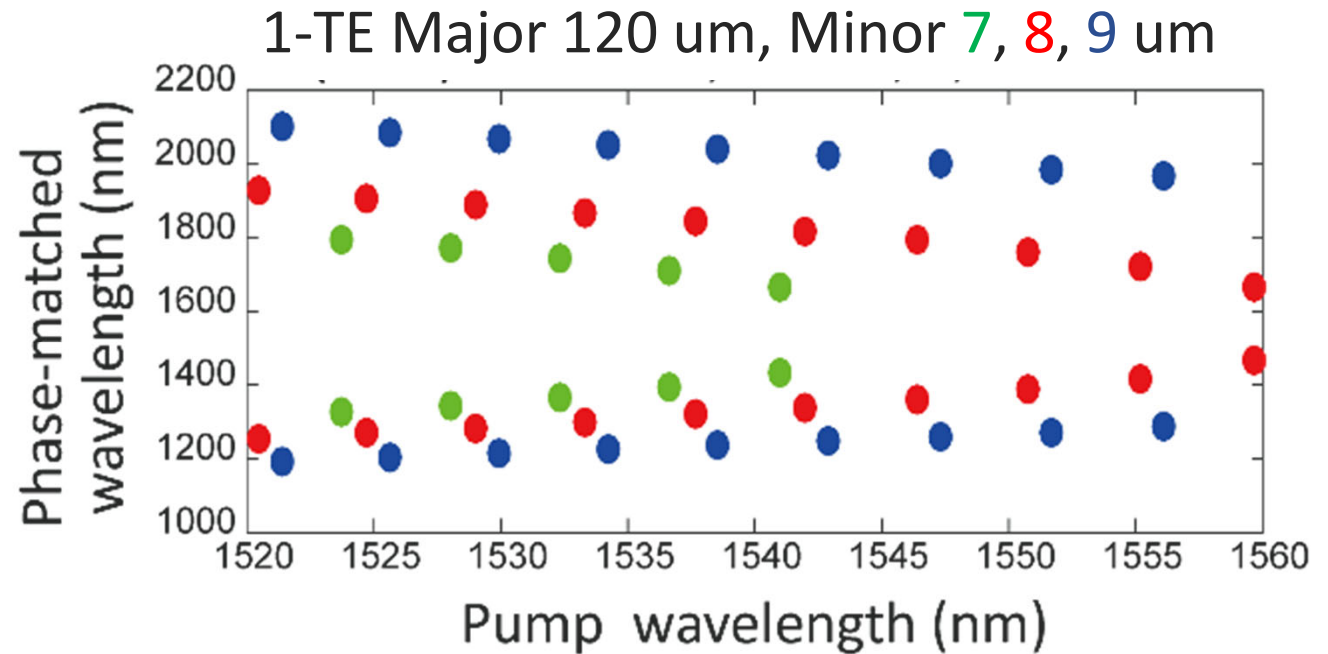
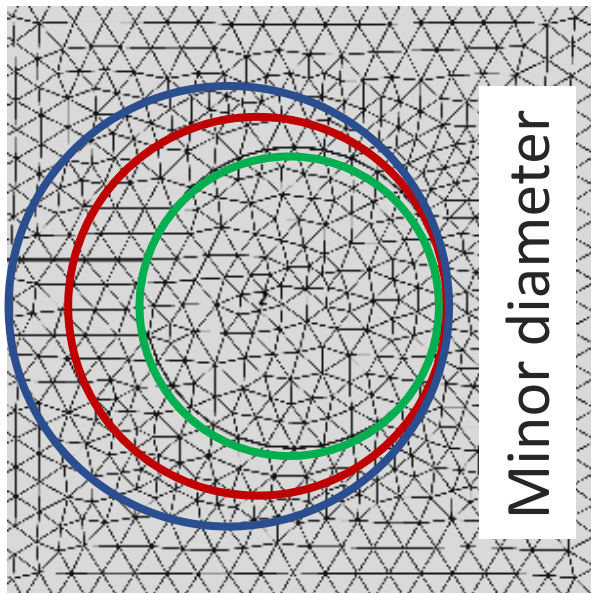


Phase-matching condition



Initial FWM occurs at the points $\Delta\omega = 0$

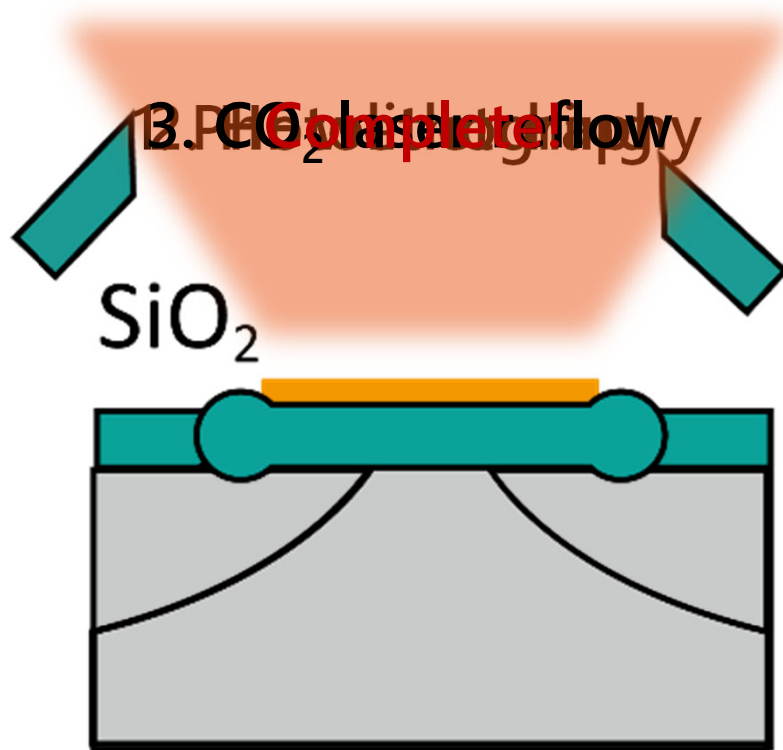
Phase-matching points depending on cavity geometry



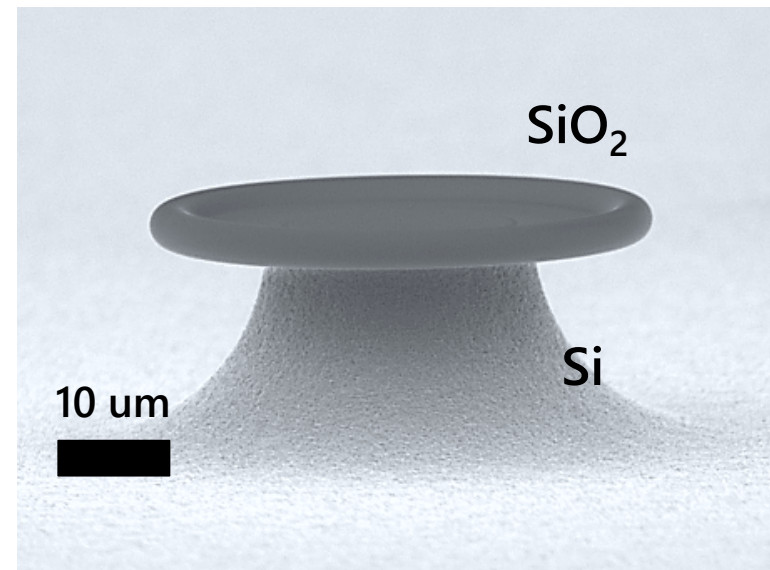
Phase-matched wavelength can be controlled by changing pump or geometry

This method offers chip-scale arbitrary frequency generators (convertors)!

Fabrication process of silica toroid microresonator



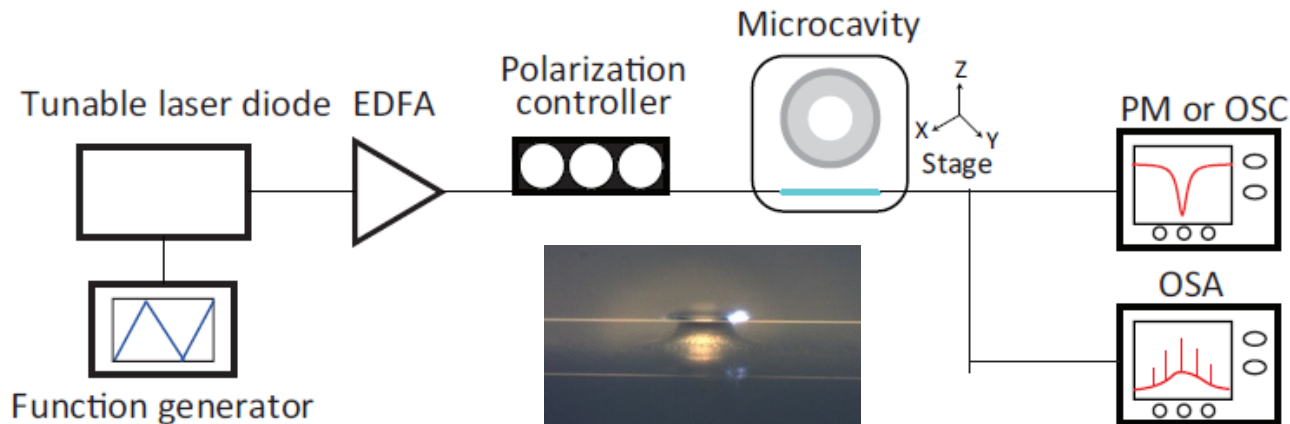
(Major diameter 20~200 μm)
(Minor diameter 3~12 μm)



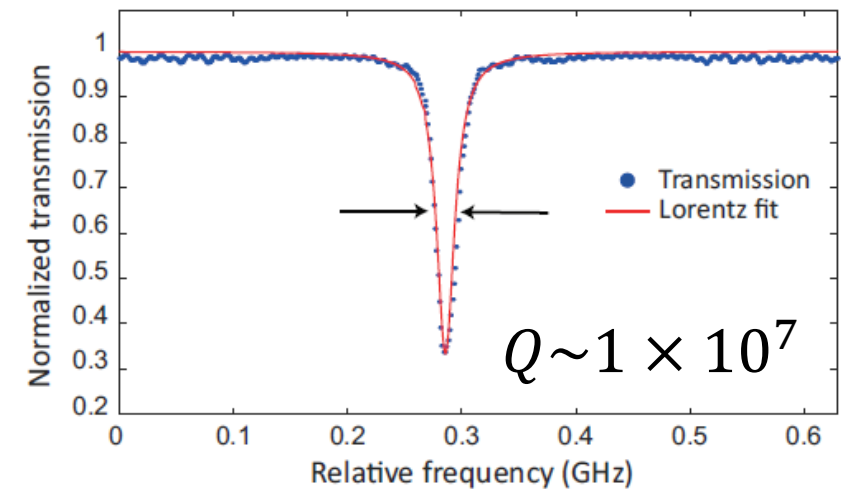


Experimental setup and optical properties

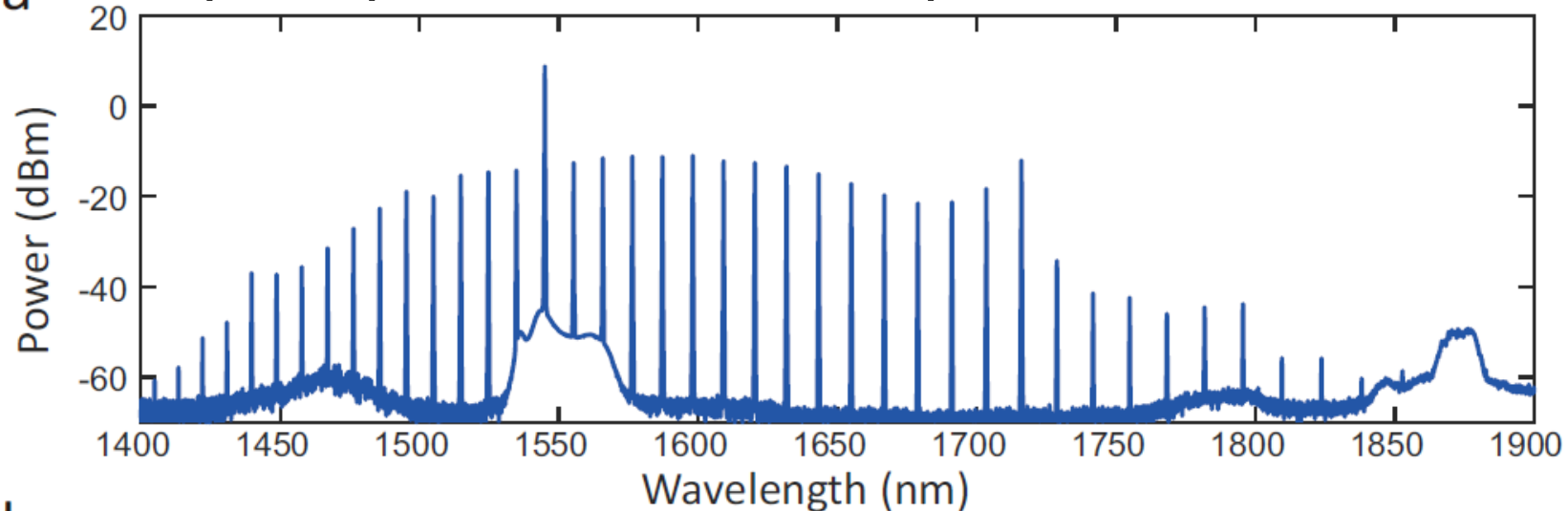
Experimental setup



Transmission spectrum



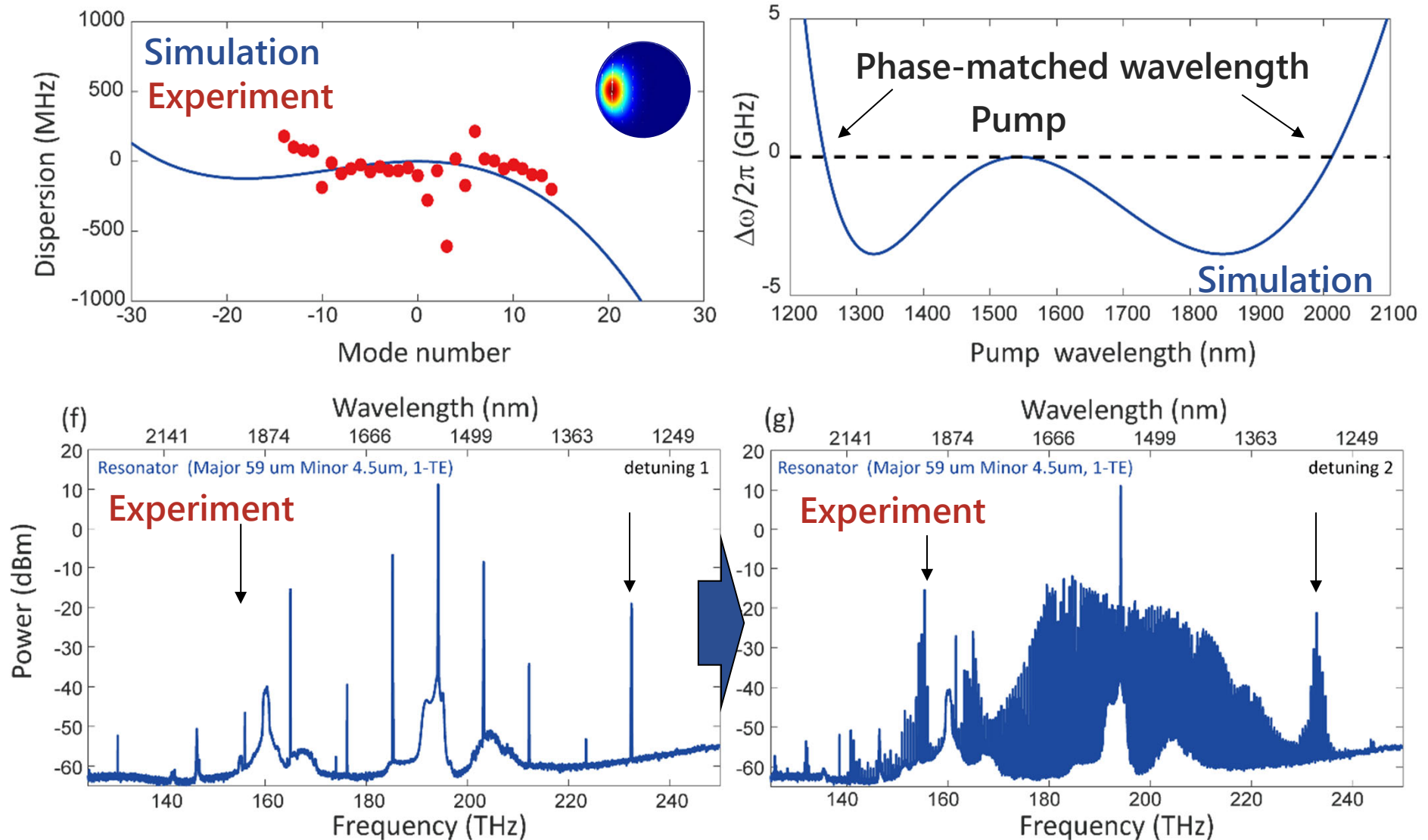
a Optical spectrum (anomalous dispersion Kerr comb)





Observation of OPO in Resonator A

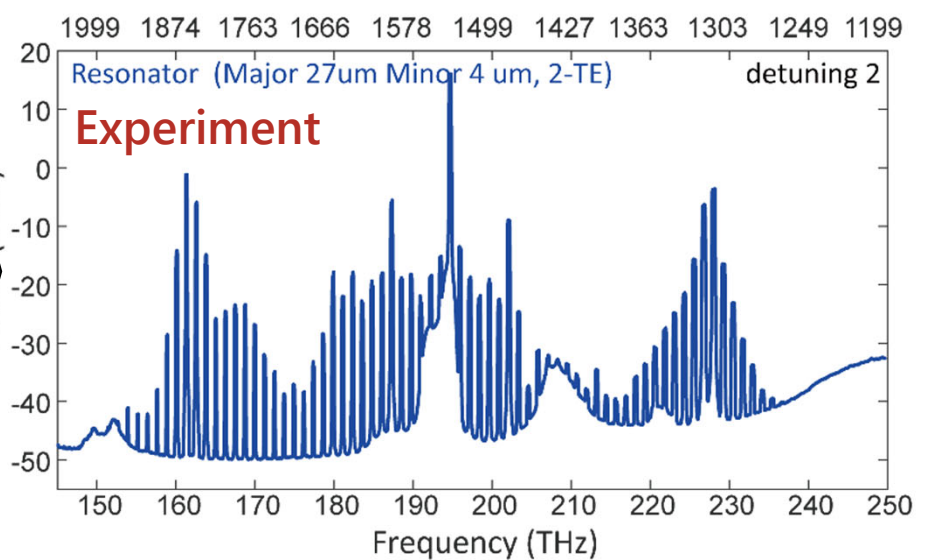
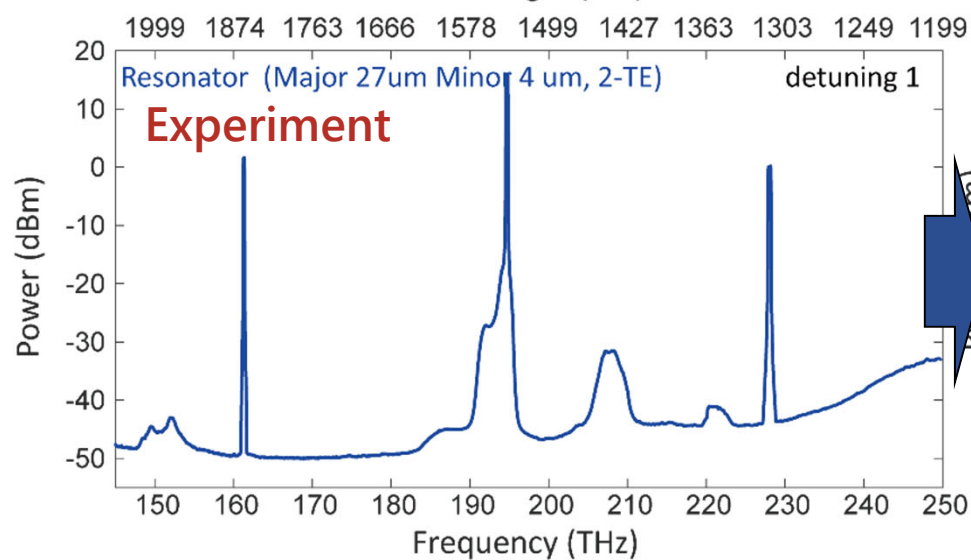
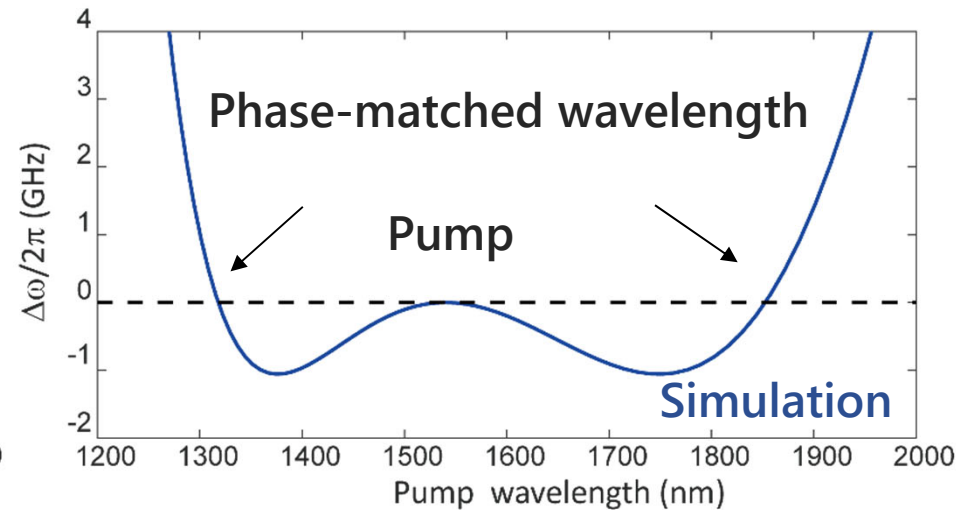
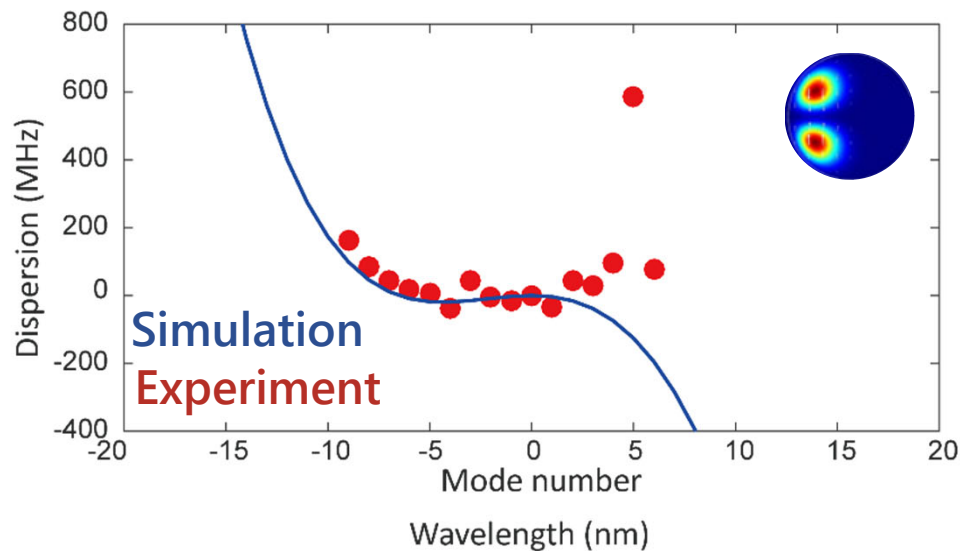
Major diameter 118 μm Minor diameter 9 μm 1-TE mode





Observation of OPO in Resonator B

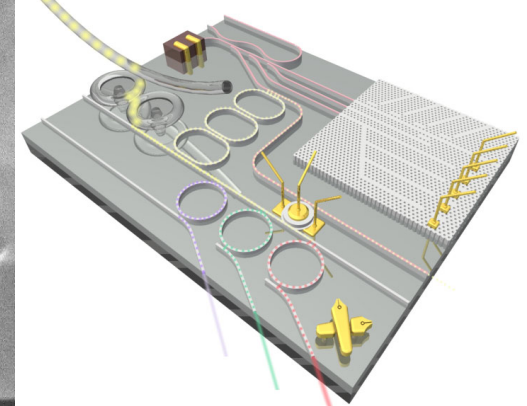
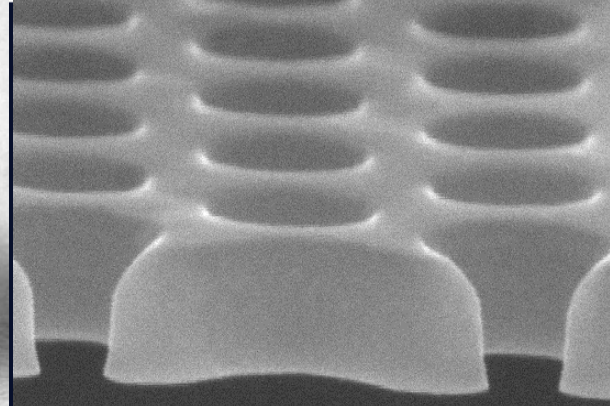
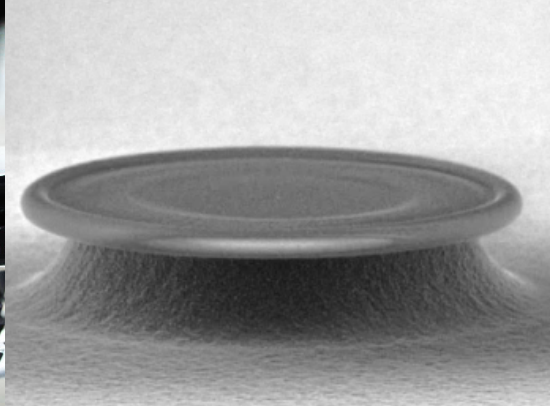
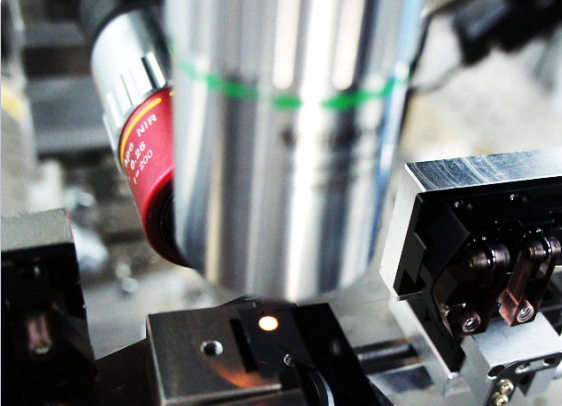
Major diameter 54 μm Minor diameter 8 μm 2-TE mode





Summary

- ◆ Demonstrated optical parametric oscillation in on-chip high-Q silica toroid microresonator
- ◆ Investigated the dependence of phase-matching condition on pump wavelength and cavity geometry
- ◆ Observed pure OPO signals and broadband four-wave mixing light by changing the pump wavelength



Thank you for your attention

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